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RF Power Circuit Designs for Wi-Fi Applications

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RF Power Circuit Designs for Wi-Fi Applications

by

Krishna Manasa Gollapudi

A thesis submitted in partial fulfillment
of the requirements for the degree of
Master of Science in Electrical Engineering
Department of Electrical Engineering
College of Engineering
University of South Florida

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DEDICATION

This thesis is dedicated to my parents who taught me to achieve anything step by step and helped me thrive. My sister who constantly urged me to give my best and my brother who has always had my back.

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I would like to thank my advisor Dr. Stephen E. Sadow who guided me throughout this research from inception. I want to express my gratitude to Dr. Gokhan Mumcu and Dr. Jing Wang for their input and patience. I am deeply grateful for my Senior Engineer, Steven Chung for providing me an opportunity of working as an intern at Global ETS, LLC. I feel blessed to have learnt Microwave and RF courses from the Department of Electrical Engineering and helped me pave the path of success.

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ABSTRACT

In the field of RF/Microwave Engineering, the Wilkinson Power divider is a passive device frequently used for splitting or combining signals. The power fed to the input port is equally or unequally split between N output ports and delivers better performance by achieving isolation between the output ports while matching all the ports. The design comprises simple transmission lines and provides power divider characteristics with the help of quarter wavelength transmission lines with different topologies.

This thesis describes the design and fabrication of lumped and N way power splitter working at an operating frequency of 2.4 GHz. These circuits are designed with Advanced Design System Software (ADS) by adopting novel Wilkinson's Power Splitter/ combiner design and are fabricated using microstrip fabrication techniques. The objective of this thesis is to design a 2-way power divider with different topologies and thoroughly compare the microstrip layout impact on isolation and return losses.

CHAPTER 1

INTRODUCTION

1.1 Motivation

Power dividers played a prominent role in the field of microwaves for many years and their basic function is to combine or divide the power entering the input port into N output ports as required. Some of the applications of these dividers are parallel distribution of low power signals into antenna arrays and to measure the intermodulation distortions with appropriate phase relationship to combine signals from a source as a combiner [1] and in transceiver systems to provide the local oscillator signal to both the transmitter and receiver circuits. Power dividers are generally thought of as microwave equipment, and typically constructed with an equivalent impedance of 50Ω at each port. Power is divided equally between the ports from a uniform transmission line feed. They ideally provide a good impedance match at both the output ports when the input is terminated with the network's characteristic impedance, usually 50Ω . After achieving an optimum impedance match to the source feed, a power divider is used to split the input into equal signals for comparison measurements. Since power dividers are bi-directional, they can also be used as power combiners. Dividers are also used to measure different characteristics of signals like frequency and power for broadband signal sampling.

The objective of this thesis is to design, fabricate and analyze the performance of a two-way power divider for Wi-Fi applications. This design selected was adopted from Wilkinson's novel design of power combiners, working with an operating frequency of 2.4 GHz since the IEEE Wi-Fi standard IEEE 802.11 operates at this frequency [2]. Advanced Design System™ software

from Agilent was used as a tool in designing the circuit schematic and corresponding layout. Scattering parameter matrices for the device were studied and analyzed to draw conclusions about the dependency of the isolation and return losses on the microstrip layout of the circuits. It was typically claimed that the straight, parallel quarter wavelength transmission lines exhibit degradations in isolation when compared to curved quarter wavelength transmission lines when ignoring the effect of coupling between the quarter wavelength transmission lines. A thorough study on these designs was performed to determine the effects of designs on isolation and return losses.

The inspiration for this thesis was the application of power combiner/divider circuits in wireless communication systems to improve the wireless signals (Wi-Fi signals) in a transceiver system. Since there are places where the wireless signals cannot reach, such as outdoor areas, large office spaces, etc. wireless repeater circuits are required. The technology for radio frequency wireless local area networking is called Wi-Fi and is based on the IEEE 802.11 standard.

1.2 Wireless Communication

Wireless communication is the transfer of data or power between two or more points, that are not connected through a wire. Simply, wireless communication is the data communication performed wirelessly [3]. Usually, wireless technologies employ radio waves as the means of communication. This is due to their ability to travel millions of kilometers for deep space radio communications or few meters for Bluetooth applications. Different types of fixed, mobile or portable applications like cellular phones, two-way radios, wireless computer mice and keyboards, etc., are enclosed by wireless communications. This term was first used in 1890 for radio transmitting and receiving technology as in wireless telegraphy until it was replaced by radio in the 1920s [4][5]. Due to the emergence of broadband communication, Wi-Fi and Bluetooth, the term wireless became the primary usage in the 2000s. In the telecommunications industry, wireless

operation permit services such as long-range communications, that are impossible to achieve using wires by employing radio transmitters, receivers, and remote controls by using energy to transfer the data without using the wires over short and longer distances [6]

A wireless network can refer to a computer network that uses wireless data connections between network nodes, which is either a redistribution point or a communication endpoint in telecommunication systems. Wireless telecommunications are implemented using radio waves as a form of communication called radio communication. Some of the examples of wireless networks include cellular phone networks, wireless Local Area Networks, wireless sensor networks and terrestrial microwave networks, the networks which uses earth-based transmitters and receivers in low frequency range [7].

Wireless PAN (Wireless Personal Area Network), Wireless LAN (Wireless Local Area Network), Wireless MAN (Wireless Metropolitan Area Networks), and Wireless WAN (Wireless Wide Area Network) are some of the wireless networks.

- Wireless PAN: This is a personal network, that connects the devices in smaller areas within a person's reach. The applications like Bluetooth and ZigBee are popular for these networks.
- Wireless LAN: Wireless local Area networks link two or more devices using a wireless distribution method over shorter distances, providing internet access through access points.
- Wireless MAN: When several Wireless LANs are connected, the wireless network is called a Wireless Metropolitan Area Networks. The IEEE standard for one of the Wireless MAN i.e. WiMAX is 802.16 [8].
- Wireless WAN: These networks cover large areas and can be used to connect to branch offices of businesses [9] or provide internet access to public systems. The wireless

connections between these access points are usually microwave links using parabolic dishes in the 2.4 GHz and 5.8 GHz bands.

Employing radio waves is the most common method of transferring information wirelessly. Wireless communication is achieved by generating and then transmitting electromagnetic waves and then receiving these waves at a remote destination through the air at the speed of light. Since the radio signal wavelength is proportional to frequency, shorter wavelength corresponds to higher frequencies. Usually, radio waves are measured in cycles per second with the common designation of Hertz (Hz for short). Hence, signal travel at great distances typically uses longer wavelengths and the penetration of longer wavelength signals through, and around, objects are better than shorter wavelength signals. Indeed, short wavelength radio communication is referred to as 'line of sight' for this reason since any obstruction (trees, buildings, etc.) greatly degrade the power transmitted to the remote receiver. This process of transmitting and receiving radio signals through wireless networks involves RF devices, principally a transmitter and receiver. These devices are often combined into a single piece of RF gear and called transceivers when in a single package. Usually one of these devices is silenced while the other functions. For example, in a radio transceiver, the transmitter is silenced while receiving the signals so as not to saturate the receiver, etc.

1.2.1 Performance of Wireless Transmitters and IEEE Standards

Wi-Fi stands for wireless fidelity and is a specific method to connect users, such as computers, tablets, smart phones, etc., to the internet, according to the IEEE's set of wireless standards. These standards describe the set of services and protocols followed by the Wi-Fi transmission networks. The most commonly encountered set of standards is IEEE Standard 802.11 wireless LAN (WLAN) and mesh. This family of specifications initially started in the 1990s and continues to evolve. These standards specify the improvements that boost wireless range and

addresses technologies that reduce power consumption. Amendments introduced during the evolution of the standards include 802.11 n, 802.11 ac and 802.11 ax, which support higher data rates by adopting higher-order modulation schemes. To maintain higher data rates, attempts were made to improve the spectral efficiency and multi-user techniques like MU-MIMO and OFDMA which have been introduced to improve network capacity and spectral frequencies (bits of data transmitted per second through 1 Hz of RF spectrum). The following table summarizes the IEEE standards from obsolete to newer amendments:

Table 1: Evolution of IEEE Wi-Fi Standards [3], [9]

Specification	802.11a	802.11b	802.11g	802.11n	802.11ac	802.11ax
Year released	1999	1999	2003	2009	2014	Expected in 2019
Operating Band	2.4 GHz	5 GHz	2.4 GHz	2.4 and 5 GHz	5 GHz	2.4 and 5 GHz
Channel Bandwidth	20 MHz	20 MHz	20 MHz	20/40 MHz	20/40/80/160 MHz	20/40/80/160 MHz
Physical Layer rate	11 Mbps	54 Mbps	54 Mbps	600 Mbps	6.8 Gbps	10 Gbps
Link Spectral Efficiency	0.55 bps/Hz	2.7 bps/Hz	2.7 bps/Hz	15 bps/Hz	42.5 bps/Hz	65.5 bps/Hz

The operational range of wireless signals depends on factors like frequency band, sensitivity of receiver, antenna choice (transmitter and receiver) and modulation technique. Additionally, propagation characteristics of signals have a strong impact on their strength. At large

distances and with greater signal absorption, signal speed is usually reduced. Generally, the maximum power that a Wi-Fi device can transmit is limited by local regulations like such as the Federal Communications Commission (FCC) in the United States and Equivalent isotropically radiated power in the European Union limit the maximum power to 20 dBm or 100 mW [3].

1.2.2 Radio Frequency Transceivers

A typical wireless transceiver has a transmitter circuit which transmits the data in the form of radio signals and a receiver circuit. The communication system consists of a transmitting and receiving antenna to transmit and receive radio signals, respectively, low noise amplifiers (LNAs) to boost the received signals while maintaining a constant signal to noise ratio (SNR), filters to remove undesired signals, mixers and local oscillators to up/down convert the signals and power amplifiers (PAs) to amplify these signals and transmit them. The block diagram of an RF transceiver system is shown in Figure 1.

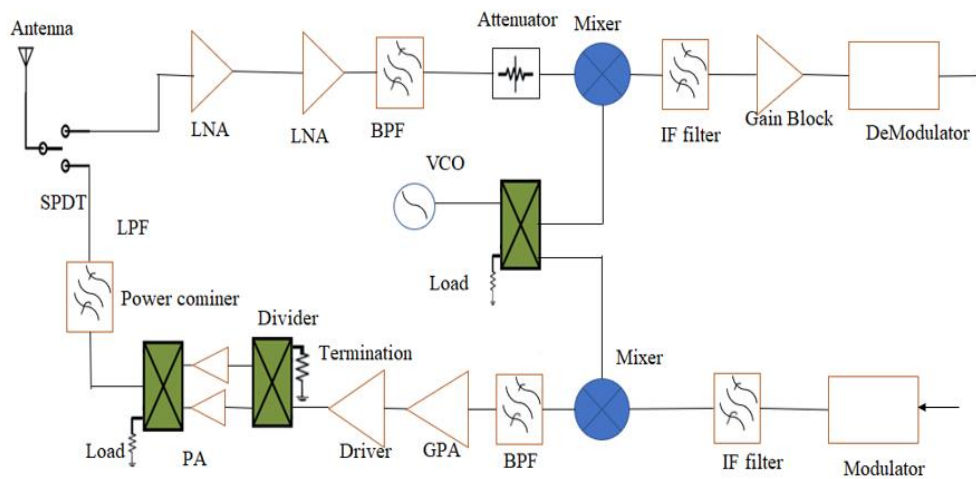


Figure 1: Block Diagram of Basic Transceiver System.

The VCO feeds the transmitter (bottom) and receiver (top) circuits. The antenna is both transmit/receive and the SPDT switches between transmit mode (connecting bottom path to the antenna) and receive mode (connecting the top path to the antenna).

The transceiver system consists of transmit and receive modules working at an operating frequency of 2.4 GHz. The signal received, or transmitted, by the antenna is controlled by the Single Pole Double Throw (SPDT) switch. The receiving system is silenced when the switch is connected downwards since the bottom half of circuit is the transmitting circuit. The local oscillator signal generated by a voltage-controlled oscillator (VCO) which is connected to a power divider. This divider splits the power received from the VCO into two signals and sends the local oscillator signals to both the mixers in the transceiver circuit. Then this signal is fed to the mixer along with the input signal from the antenna. This input signal initially is amplified by two low noise amplifiers (LNAs) while improving the Signal to Noise ratio (SNR) through a band pass filter to filter out the low frequency components and pass the center frequency [11]

The transmitting circuit is represented in figure 3. The antenna in the receive module receives the signals from the mixer to amplify and filter the signals with the frequency other than the desired frequency, usually high frequency signals. This filter is called intermediate filter and the signals intermediate signals. These signals are then amplified at the output by an amplifier. This receiver circuit is shown in the figure 4.

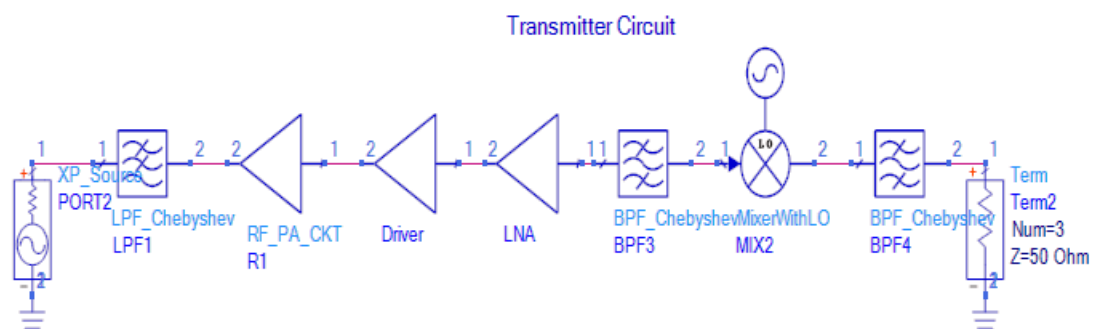


Figure 2: Schematic Diagram of Transmitter Circuit.

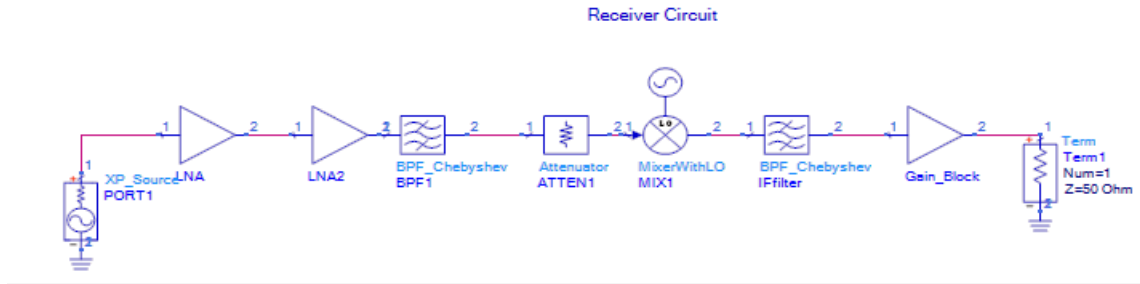


Figure 3: Schematic Diagram of Receiver Circuit.

Usually, this device comprises both transmitters and recovers in a common circuit. If there is no common circuit between a transmitter and receiver the device is a transmitter-receiver. There are some devices like transponders, transverters and repeaters that share this principle.

1.2.3 Repeaters

In the field of telecommunications, repeaters are the devices that receives a signal and retransmits it electronically. These devices are used to extend signal transmission so that the signal will be received by the other side of obstruction or cover longer distances. Some of the repeaters broadcast a similar signal but alter the method of transmission of the signal via a change in frequency or baud rate (baud rate is the modulation rate in pulses, or symbols, per second). Depending upon the type of data handled, repeaters are divided into two categories, analog or digital repeaters. There are other types of repeaters such as telephone repeaters, optical communications repeaters and radio repeaters. The optical repeater is used to amplify the light beam in an optical fiber cable, a telephone repeater in a telephone line acts an amplifier [12], and a radio repeater can retransmit a radio signal by acting as both radio transmitter and receiver. Finally, there is the wireless repeater, which is used to extend the wireless range of existing signals and rebroadcast it. The most commonly used repeater in mobile communications is a cellular repeater, which is a type of radio repeater used for boosting the cell phone reception in an area.

Usually cellular repeaters have a directional antenna to receive the signals from the tower, an amplifier to boost the signal which is then rebroadcast to nearby cellphones using a local antenna.

The communication coverage is improved by radio repeaters and, without a repeater, these systems have limited range due to land terrain and obstructions. Similarly, to boost or to extend the range of Wi-Fi signals wireless repeaters are often deployed. This circuit operates by taking a signal from a wireless router, or from an access point and rebroadcasting it to create a secondary network. Wireless repeaters are usually used when two or more users must be connected over longer distances when direct connection cannot be established commonly in homes and offices. These repeaters are usually employed in an environment where interference exists due to environmental factors like the presence of microwaves from the microwave oven or from the metals or from computer devices or hubs [3]. The absence of a wireless hotspot can also be one of the reasons to employ wireless repeater.

Wireless repeater circuits are also used to improve mobile communication systems to improve the coverage of the signal. Figure 4 shows the coverage of the signal by a base station and additional coverage after employing a wireless repeater circuit.

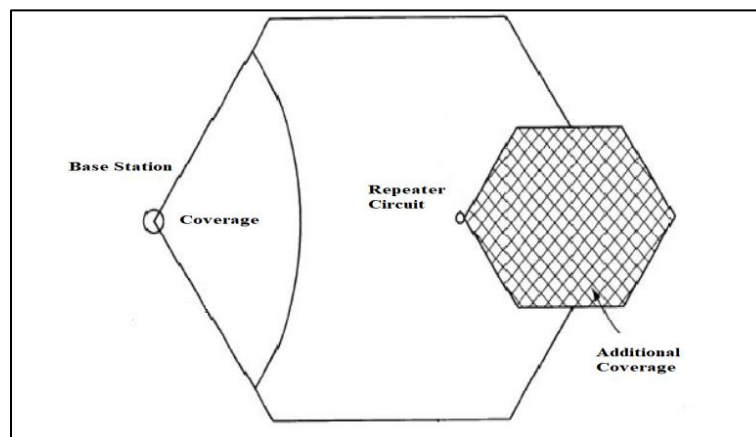


Figure 4: Mobile Communication Coverage Using a Wireless Repeater.

This arrangement helps to boost the base station to mobile user signal and mobile user to base station signal thereby increasing the data rate at the boundary of the mobile coverage area.

1.3 Objectives and Scope of the Thesis

The objective of this thesis is to design a wireless repeater circuit to boost signals on an as-needed basis. This was accomplished via n-way Wilkinson power divider circuits, with different topologies implemented using Advanced Design System (ADS) software. These circuits can have different layout configurations such as bent, curved and tapered designs. After constructing the divider circuits, they were further analyzed, and compared.

The scope of the thesis is:

- A Literature review of S-parameter matrices and different power-dividing circuit designs
- Selection of suitable power dividers
- Design of Wilkinson power Divider (3 Port) using ADS
- Comparison of the different design topologies for different Wilkinson power dividers
- Fabrication of prototype power dividers using FR4 as substrate board
- Measurement of prototype device performance with a Vector Network Analyzer
- Analysis and comparison between simulated and fabricated Wilkinson power dividers

1.4 Thesis Outline

This thesis is organized into 5 chapters. Chapter 2 covers even and odd mode circuit analysis of the Wilkinson power divider to help in understanding the performance and their corresponding S-matrices. RF devices, types of amplifiers and their design methodology, fabrication and testing methods as a part of internship experience at an electronics company, Global ETS, LLC (Odessa, FL) is discussed in Chapter 3. Chapter 4 presents the design procedure and construction methods of the dividers using Advanced Design System software. The ideal Wilkinson power divider and its performance with simple simulations are also included to help understand the limitations of this device. The design of a 2-way Wilkinson divider (with straight and bent topologies) are also included in this chapter. Finally, validation of the simulated results

obtained in previous chapters along with a brief discussion of conclusions drawn from this research and their potential future work are presented in chapters 4 and 5.

CHAPTER 2

THEORY OF POWER DIVIDERS

Power combiners couple definite amount of power in a transmission line to a port, allowing the signal to be used in another circuit. A scattering matrix helps in quantifying the electromagnetic energy propagating through a multiport network. For an RF signal incident at one port, some fraction of the power is reflected, and some enters the incident port and then scatters through all the ports. The representation of the possible input and output path of the signal in a mathematical construct is in matrix format as a scattering matrix or S-matrix. Each parameter in the matrix is a complex number, having magnitude and phase or real and imaginary parts. The rows and columns depend on the number of the ports the network has and is discussed further in this chapter.

2.1 S Parameter Matrix

Before considering the different types of power dividers commonly used in the RF industry, a better understanding of the scattering matrix (S-matrix) is required. This matrix is typically used to relate the total voltages and currents at the RF circuit ports by considering both signal magnitude and phase. Thus S-parameters provides a complete description of an N-port RF network at microwave frequencies. The S-matrix for an arbitrary N-port microwave network is written with V^- indicating the amplitude of reflected voltage waves from port n and V^+ indicating the amplitude of the incident voltage waves to port n as (1-4):

$$\begin{bmatrix} V_1^- \\ \vdots \\ V_n^- \end{bmatrix} = \begin{bmatrix} S_{11} & \cdots & S_{1n} \\ \vdots & \ddots & \vdots \\ S_{n1} & \cdots & S_{nn} \end{bmatrix} \begin{bmatrix} V_1^+ \\ \vdots \\ V_n^+ \end{bmatrix} \quad (2.1)$$

Each element in the matrix can be determined using:

$$S_{ij} = \frac{V_i^-}{V_j^+} \quad (2.2)$$

where V_j^+ is the reflected voltage wave exiting through port “i” and V_i^- is the incident voltage wave entering through port “j”. Specifically, this is the ratio of an incident wave incident on port j and a reflected wave exiting through port i. Usually, a Vector Network Analyzer (VNA) is used to measure the S parameters by considering that all the incident waves on all the ports except port j are zero. For some devices that have more than two ports, such as splitters, which usually have three, any port which is not used for measurement is terminated with a matched load. It is known that if the device is matched at all the ports the input impedance of each port is equal to the total characteristic impedance of the system, resulting in zero reflection coefficient. This means that the wave incident on the matched port will not be reflected as the reflected voltage is zero. If the matched port condition (where $i=j$) is applied to the s-matrix, the diagonal elements will be reduced to zero.

In principle power dividers are reciprocal in performance. Reciprocity is the property exhibited when the transmission of power in a device or circuit between two ports which is the same irrespective of direction of propagation through the device. Hence the equation can be represented as

$$S_{ij} = S_{ji} \quad (2.3)$$

The S-matrix elements for a reciprocal device, make the matrix symmetrical, is used to determine the losses induced by the device itself. Ideally, a lossless power divider is desired, but we can practically realize only a low-loss divider. It is proven that the device would be lossless if the elements in the S-matrix are unitary, which means that the sum of squares of elements in the rows equals one. This can be represented in product form as

$$[S]^t [S]^* = [I] \quad (2.4)$$

where $[I]$ represents a unit matrix. $[S]^t$ is the transpose and $[S]^*$ is the conjugate of S- matrix [13]. Hence, if any device follows the above condition, it is a lossless device.

The performance of a power divider can also be influenced by the isolation between output ports of the device. Isolation is the property of a device where a signal at one port does not affect the signal from another port. Usually, for a three-port power divider, to reduce the interference caused by coupling between the ports, it is necessary for the output ports to be isolated. In a power divider circuit, if port 2 and port 3 are output ports, the elements S_{32} and S_{23} relate to port isolation. These are the ports where a signal enters through port 3 and exits through 2, and vice versa. Since we need strong isolation between these ports, their magnitudes should be small.

The ideal power divider should be lossless, reciprocal, and matched at all the ports. However, it is not possible to have a lossless divider with matched ports under all conditions. To denote this, we can consider a general S-matrix as:

$$[S] = \begin{bmatrix} S_{11} & S_{12} & S_{13} \\ S_{21} & S_{21} & S_{23} \\ S_{31} & S_{32} & S_{33} \end{bmatrix} \quad (2.5)$$

Assume that the device is matched and reciprocal. By applying all the conditions mentioned above to the general s-matrix, it is modified as:

$$[S] = \begin{bmatrix} 0 & S_{12} & S_{13} \\ S_{21} & 0 & S_{23} \\ S_{31} & S_{32} & 0 \end{bmatrix} \quad (2.6)$$

Now, to prove the matching condition, the s-matrix should be unitary as:

$$|S_{12}|^2 + |S_{13}|^2 = 1 \quad (2.7)$$

$$|S_{21}|^2 + |S_{23}|^2 = 1. \quad (2.8)$$

$$|S_{31}|^2 + |S_{32}|^2 = 1 \quad (2.9)$$

$$S_{23}^* S_{13} = 1 \quad (2.10)$$

$$S_{13}^* S_{12} = 1 \quad (2.11)$$

$$S_{23}^* S_{12} = 1. \quad (2.12)$$

To satisfy the above conditions, two of the three elements S_{13}, S_{12} and S_{23} should be zero [15]. However, considering any two of these elements, all three conditions of lossless, reciprocal, and matched are not satisfied. Hence, a Wilkinson's power divider can be designed as a reciprocal and a matched device, but it is lossy.

2.2 Types of Power Dividers

In many radio frequency and microwave applications, it is necessary to divide power simultaneously to multiple circuits. This can be accomplished easily with power dividers and splitters. The difference between a splitter and divider is the configuration of the resistor used in dissipation of power in these circuits. While an ideal power divider with lossless, reciprocal, and matched properties cannot be realized physically, there some power dividers which can follow two of these properties. Some of the common power dividers like T junction dividers, resistive dividers, and Wilkinson dividers, have unique design properties. Both the dividers and splitters can be realized with quarter wave transformers, transmission lines, micro strip transmission lines or strip lines. Power dividers and splitters are not interconvertible. A power divider can also be used as a power combiner, acting as a bidirectional and symmetrical device. Common applications where a divider acts a combiner are in communication receivers where power needs to be combined from different sources and in amplifier circuits where power needs to be combined from different power amplifiers. A simple power splitter and power divider having lumped components with two resistors and three resistors, respectively, are shown in Figure 5.

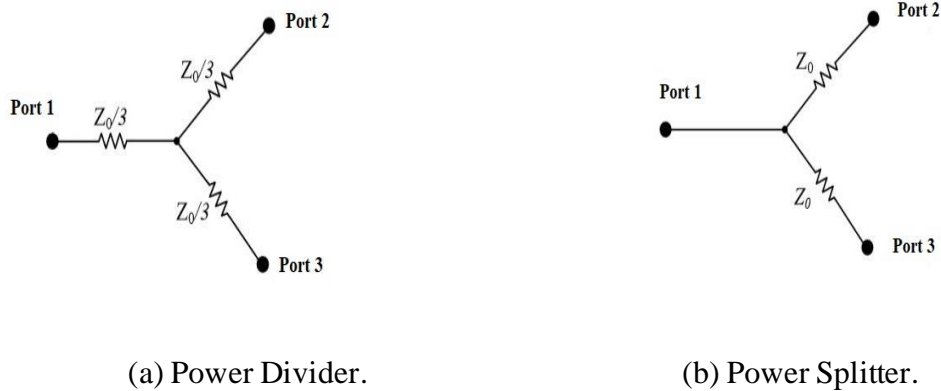


Figure 5: Power Divider and Power Splitter Schematics.

Power dividers are usually N-port devices that are lossless or, as a minimum, low loss devices. A basic three port (one input port and two output ports) device splits power equally (3 dB) into each output port. An unequal split power divider is also physically realizable. The design specifications required for a power divider in most applications are high isolation, high return losses, low insertion losses, compact size and high bandwidth.

A lossless T junction power divider can be simply designed as three transmission lines intersecting at a junction, which has reactance due to fringing fields and higher order modes corresponding to the discontinuity formed at a junction resulting in storage of energy caused by the lumped susceptance, B . The lossless T junction divider is shown in Figure 7.

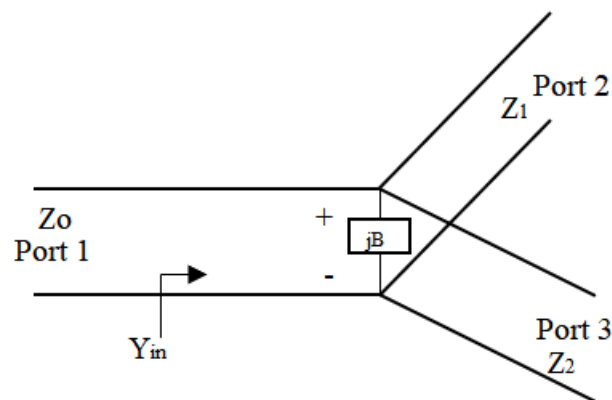


Figure 6: Lossless T Junction Power Divider Schematic.

The total impedance of this T junction divider is given by:

$$\frac{1}{Z_0} = \frac{1}{Z_1} + \frac{1}{Z_2} + jB \quad (2.13)$$

In the above equation, Z_0 is the impedance of the input port and Z_1 and Z_2 are the impedances of the output ports.

If B equals zero, we can rewrite the above equation as

$$\frac{1}{Z_0} = \frac{1}{Z_1} + \frac{1}{Z_2} \quad (2.14)$$

However, if B is not negligible, we can reduce the effect of the susceptance by using a reactive tuning element over a narrow frequency range. Since transmission lines have less losses, the required impedances to obtain respective power ratios in each section can be determined [13].

Although the lossless T junction power divider can be reciprocal, it is not matched at all ports. From the above-mentioned equation (2.14), we can deduce that it cannot be matched since one of the three impedances should differ to provide better power division. Thus, the need to adopt quarter wavelength transformers arises to provide for a matched condition. Resistive power dividers are designed to ensure that the same impedances are attained at all ports, but this introduces losses in the circuit. The typical resistive power divider is shown in Figure 7.

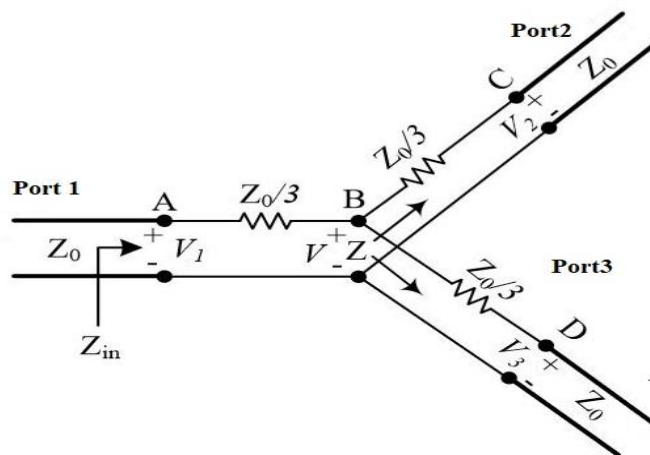


Figure 7: Three Port Resistive Divider Schematic.

If we assume that all the ports are terminated with an impedance of Z_0 , then the impedance Z , while observing at ports two and three through the $\frac{Z_0}{3}$ resistor, is determined as:

$$\begin{aligned} Z &= \left(\frac{Z_0}{3}\right) + \left(\frac{Z_0}{3} + Z_0\right) \\ &= \frac{Z_0}{3} \quad (2.15) \end{aligned}$$

The impedance observed at the input Z_{in} can be calculated as

$$\begin{aligned} Z_{in} &= \left(\frac{Z_0}{3}\right) + Z_0 \\ &= Z_0 \quad (2.16) \end{aligned}$$

Therefore, the input port is matched to Z_0 , because all the ports are symmetrical and matched, representing the diagonal elements in the S-matrix are zero. The nodal voltages can be calculated as:

$$\begin{aligned} V &= V_1 * \left(\frac{\frac{2Z_0}{3}}{\frac{2Z_0}{3} + \frac{Z_0}{3}}\right) \text{ At node B} \\ &= \frac{2V_1}{3} \quad (2.17) \end{aligned}$$

$$\begin{aligned} V_2 = V_3 &= V_1 * \left(\frac{Z_0}{Z_0 + \frac{Z_0}{3}}\right) \text{ At Node B and C} \\ &= 0.5 * V_1 \quad (2.18) \end{aligned}$$

The power at the input port can be written as:

$$P_{in} = \frac{1}{2} \frac{V_1^2}{Z_0} \quad (2.19)$$

Since, we considered an equal split power divider, the power at the output ports is:

$$P_2 = P_3 = \frac{1}{8} \frac{V_1^2}{Z_0} \quad (2.20)$$

Output powers P_2 and P_3 equal half of the input power. Half the power from the input is divided between the output ports while the remaining half is dissipated through the resistors [13]. Further, it should be noted that isolation is observed at the output ports.

2.2.1 Wilkinson's Power Divider

Although the T junction power divider is lossless, it cannot exhibit matching at all ports and it has no isolation, while resistive splitters are lossless and can be matched at all the ports but doesn't exhibit isolation. Hence, Ernest Wilkinson proposed a power divider in 1960 that provides high isolation between the output ports and matches all the ports. This design becomes lossless when the output ports are matched. The design consists of a transmission line, split into the desired number of outputs with the transmission lines each being a quarter wavelength long. Usually, they are strip or micro strip transmission lines. There are resistors between each transmission line and at the junction of the transmission lines. Since the voltages along these transmission lines have the same magnitude and phase when connected to a matched load, there will be no power dissipation observed through the resistors due to the absence of a voltage drop. The typical circuit diagram for the Wilkinson's power divider is shown in Figure 9

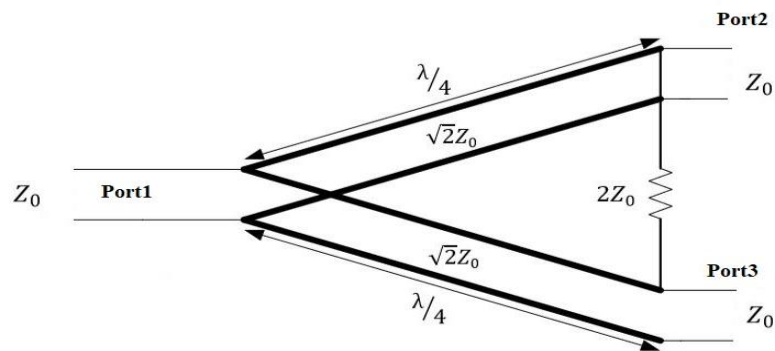


Figure 8: Transmission Line Model of Wilkinson Power Divider.

The impedance of each quarter wave transmission line is equal to the characteristic impedance of the input transmission line multiplied by a factor of $\sqrt{2}$. There is also an internal resistor between two output ports, whose impedance is twice the impedance of the input

transmission line. These impedances help isolate the output ports of the divider while matching the input [7]. The S-matrix for a typical divider with the above-mentioned properties can be given as:

$$[S] = \frac{-j}{\sqrt{2}} \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{bmatrix} \quad (2.21)$$

This matrix represents power entering through port 1 being divided between port 2 and port 3. Since the ports are matched, S_{11} , S_{22} and S_{33} are zero. We know that for any lossless device, the sum of the squares of the first column elements in the S-matrix are unitary [13].

It is observed that when the signal is applied at port 2, half of the power of the incident signal is observed at port 1 while the other half is dissipated through the resistor connected at the junction, but reciprocity is attained. Hence, $S_{21} = S_{12}$. Due to the isolation between the output ports, we cannot observe any power at port 3 when signal is applied at port 2 for an ideal Wilkinson divider.

If two signals with the same amplitude and phase are applied at both output ports, port 2 and port 3 of an equally split Wilkinson divider, the sum of incident signals is observed at port 1, the input port. This is because, the signals are in phase and no power is dissipated through the resistor. These signals interfere constructively at the junction so, the divider acts as a power combiner.

Wilkinson power dividers can be cascaded, or a single divider can have many output ports. When a divider is cascaded to obtain multiple output ports, isolation between the output ports is more likely to be maintained. The characteristic impedance of the quarter wave transmission line ($Z_{\lambda/4}$) for a given number of output ports n , an input impedance R_s , and load impedance R_L is given as:

$$Z_{\lambda/4} = \sqrt{n R_s R_L} \quad (2.22)$$

Furthermore, as the number of output ports increases, the isolation between these ports decreases [17]. Table 2 gives the information about the effect of isolation and theoretical insertion loss with number of output ports.

Table 2: Isolation and Insertion Losses for Number of Output Ports [17] [15].

Number of output ports	Theoretical Insertion Loss (dB)	Isolation (dB)
2	3	∞
4	6	21.6
6	7.8	17.6
8	9	16.1
3	4.8	∞
5	7	19.5

Due to the lossless nature of the power divider under matched conditions, and the ease of designing and constructing the circuit using micro strip lines, the Wilkinson power divider is an ideal design to employ power division and is further studied.

2.3 Even and Odd Mode Analysis on Wilkinson Divider

The performance of the divider can be analyzed with the effects of even and odd mode impedances of the coupled lines on the S parameters, since impedance is a vector quantity which is the ratio of electromagnetic voltage to current. To obtain the S-matrix, incident and reflected voltages, we employed superposition and circuit symmetry. Initially, a Wilkinson divider with source voltage of V_g at port 2 is considered and the rest of the ports are matched with impedance of Z . The circuit schematic is shown in Figure 10. To simplify this schematic, the ground plane is removed, which includes the bottom conductor of the transmission lines [15] [16].

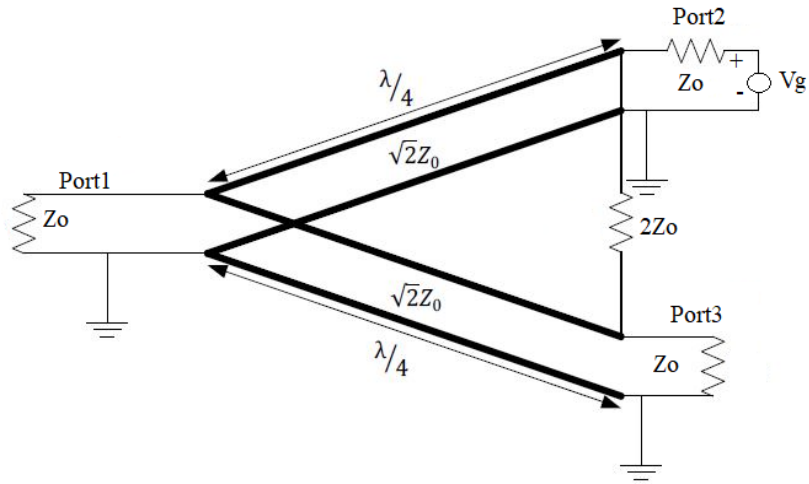


Figure 9: Schematic of the Divider with Source at Port 2.

The voltage at port 2, V_g , is split into two sources in series each of voltage $V_s/2$ and at port 3, we can draw two additional sources of voltages $+V_s/2$ and $-V_s/2$. The schematic in Figure 5 can be redrawn with these sources at port 2 and 3. Since incident and reflected voltages at each port are essential to derive the S-matrix, we can assume the total voltage at ports 1, 2 and 3 as V_1 , V_2 and V_3 , respectively. The modified schematic is shown in Figure 11.

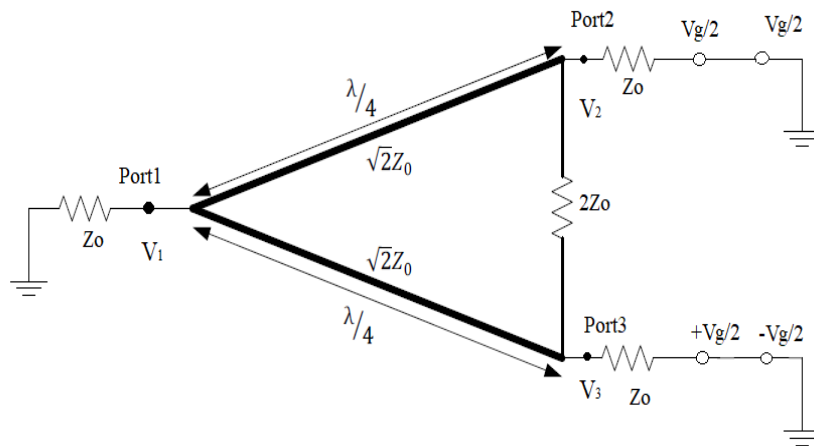


Figure 10: Wilkinson Divider with Source Voltages at Ports 2 and 3 and the Load at Port 1 (i.e., Using the Wilkinson Divider as a Power Combiner).

2.3.1 Even Mode Analysis of Wilkinson's Divider

To find the even mode voltages, in the above Figure 5, we turned off one of the voltages in port 2 ($V_g/2$) and the negative voltage ($-V_g/2$) in port 3. The remaining sources in the schematic at the output ports are equivalent and, due to this, the current does not flow in the plane of symmetry which is the plane which bisects the circuit. This creates a virtual open along the plane of symmetry, which is shown in Figure 12. For evaluating this circuit, the resistor at the input port, port one is split into two shunt resistors with impedances of $2Z_0$ and the resistor between output ports is divided into two series resistors of equal resistances of Z_0 . The voltages here are represented by a superscript of "E" to denote the even mode voltage at respective points. [16].

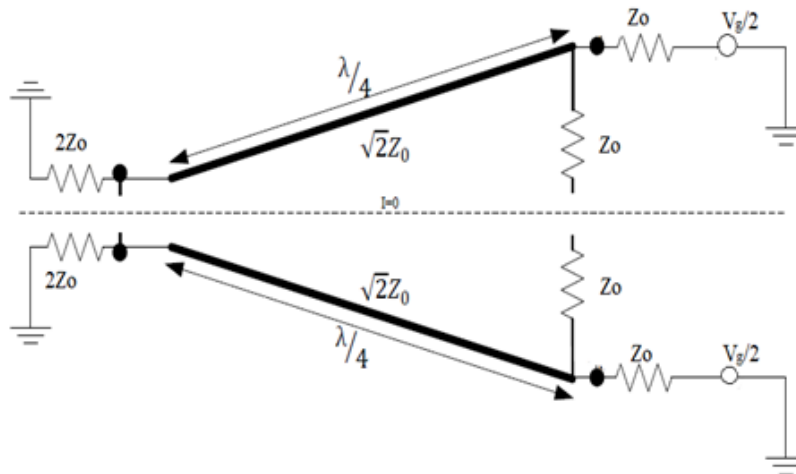


Figure 11: Even Mode Wilkinson Schematic Circuit with Virtual Open.

The top and bottom halves of the circuits can be drawn individually using the plane of symmetry in Figures 8 and 9 from the circuit in Figure 12. These circuits can be modified into an equivalent circuit due to the presence of quarter wavelength transmission lines and the port voltages can be determined by the Figure 12b.

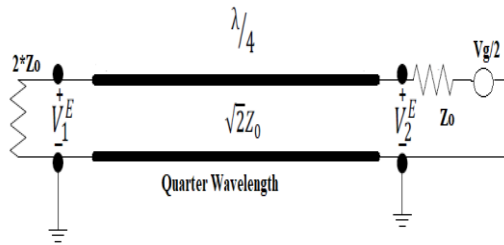


Figure 12a: Half Circuit of Even Mode

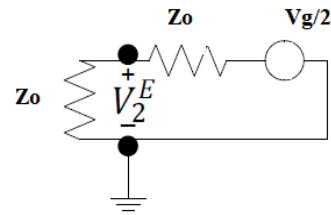


Figure 12b: Simplified Even Mode Circuit.

Wilkinson Divider.

The voltages at the end of each node was determined by voltage division and, since these circuits are identical for even mode, the voltages are $V_g/4$ for V_2^E and V_3^E . The value of V_1^E cannot be determined directly and hence, we apply voltage division across the $2Z_0$ resistor and by multiplying the resistance and current flow across the voltage drop as $-jV_g/2\sqrt{2}$. [15].

2.3.2 Odd Mode Analysis of Wilkinson's Divider

The odd mode symmetry is observed when the even sources are turned off in the equivalent circuit of the Wilkinson's divider showed in Figure 10. Along the line of symmetry, i.e. where the circuit is divided into symmetrical sub circuits, the voltages at port 2 and 3 cancel out because they are 180 out of phase, which results in the formation of a virtual ground. Like the even mode analysis, we can split the resistor at port 1 to two shunt resistors, each of value $2*Z_0$. The voltage at node 1 is split into two nodes but since there is only one node, we can represent this with a short circuit between the nodes. The resistor between the output ports 2 and 3, is divided into resistors of equal resistance Z_0 in series. Since we are analyzing the odd mode divider, the voltages V_1 , V_2 and V_3 are now represented with a superscript "O" [15]. The equivalent odd mode Wilkinson's divider is shown below Figure 13.

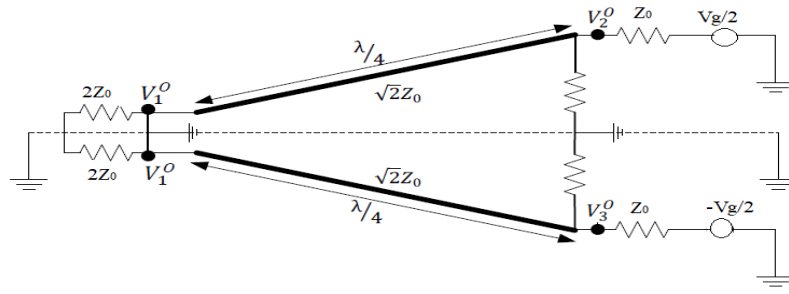


Figure 13: Equivalent Circuit of the Odd Mode Wilkinson's Divider.

The transmission line in the above figure is terminated with a short circuit, thus the input impedance can be determined as.

$$Z_{in} = Z_0 \frac{Z_L + jZ_0 \tan \beta l}{Z_0 + jZ_L \tan \beta l} \quad (2.23)$$

here, Z_0 is the characteristic impedance of quarter wave transmission line, Z_L is the load impedance of the short-circuited line and β is the electrical length, equal to $2\pi/\lambda$. Hence, the input impedance can be written as

$$Z_{in} = \frac{Z_0^2}{Z_L} \quad (2.24)$$

In the odd mode analysis, the voltages can be easily determined with voltage division and the voltages at the second and third ports are V_2^o and V_3^o are $V_g/4$ and $-V_g/4$, respectively, and the voltage at port 1 is V_1^o which is 0. The odd mode and even mode voltages at each port are written in the following Table 3.

Table 3: Port Voltages of Odd Mode and Even Mode Analysis of Wilkinson's Divider

Port voltages		Odd mode Analysis	Even mode Analysis
V_1^o	V_1^E	0	$-jV_g/2\sqrt{2}$
V_2^o	V_2^E	$V_g/4$	$V_g/4$
V_3^o	V_3^E	$-V_g/4$	$V_g/4$

By applying the principle of superposition, the even mode and odd mode port voltages are summed up to get the total voltages as shown in Table 4. After determining these, we can derive the scattering matrix by observing the incident and reflected voltages at all ports. But since ports 1 and 3 are matched, the supply is given to port 2 as shown in Figure 10.

Table 4: Voltages at Each Port of Power Divider

Ports	Total voltages	Incident voltage	Reflected voltage
1	$-jVg/2\sqrt{2}$	0	$-jVg/2\sqrt{2}$
2	$Vg/2$	$Vg/2$	0
3	0	0	0

If the source is given at port 3 instead of port 2, we can derive the values in the third column of the s-matrix. This is due to the bilateral symmetry of the Wilkinson's divider. Hence, S_{12} is equals S_{13} , S_{23} equals S_{32} and S_{22} equals S_{33} . Since Wilkinson's dividers are reciprocal, when the source is at port 1, the values of S_{21} and S_{31} are equal to S_{12} and S_{13} . We know that the source matched at port is 0 i.e. S_{11} is equal to zero [16].

$$S_{12} = \frac{V_1^-}{V_2^+} = \frac{-jVg}{\sqrt{2}} \quad (2.25)$$

$$S_{22} = \frac{V_2^-}{V_2^+} = 0 \quad (2.26)$$

$$S_{32} = \frac{V_3^-}{V_2^+} = 0 \quad (2.27)$$

Hence the scattering matrix of the Wilkinson's divider is derived as

$$[S] = \frac{-j}{\sqrt{2}} \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{bmatrix} \quad (2.28)$$

When the source is driving Port 2 of the power divider, we can see that only half the power is transmitted to the load (Port 1) since half the power is dissipated through the resistor. The same result is observed when driving Port 3 as shown by equations 2.29 and 2.30.

$$[S] = \frac{-j}{\sqrt{2}} \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \quad (2.29)$$

$$[S] = \frac{-j}{\sqrt{2}} \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{bmatrix} \quad (2.30)$$

It can be observed that the power divider is lossy when the sources are applied at Port 2 and Port 3 separately. However, when the power source is applied at both Ports 2 and 3 simultaneously, we observe that the power divider acts as a power combiner due to the reciprocity property of the device. This is possible because the incident voltage waves are in-phase and thus add constructively in the device.

$$[S] = \frac{-j}{\sqrt{2}} \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{bmatrix} \quad (2.31)$$

The scattering matrix of Wilkinson's power divider and combiner were derived, and the performance characteristics of the device were also studied by incorporating the concepts of superposition and conducting even mode and odd mode analysis. Since scattering matrix has incident and reflected voltages, by supplying sources to one of the ports and by matching another port, we derived the incident and reflected voltages at each mode and constructed a scattering matrix, which shows the performance of the power divider at the given frequency and the characteristic impedance of the system since, the elements in matrix vary as function of frequency.

CHAPTER 3

RF TRANSISTORS TESTING

An amplifier is an electronic device used to increase the magnitude of the input signals. The amplification is measured in terms of gain. Voltage, current or power can be amplified, the gain of an amplifier is the ratio output signal's (voltage, current or power) compared to the original input signal. These are active devices which depend on the input power of the signals and are used widely in wireless communications and in broadcasting to boost the received signals. The signal received by the receiver plays a major role in determining the strength of the communication link. However, the signal transmitted by the transmitter has low power and high noise, to achieve better communication power of the signal should be amplified, and noise should be reduced after receiving the signal, which is accomplished by using amplifiers. Depending upon their functions, amplifiers are divided into four types and are discussed further in this chapter.

3.1 RF Transistor Validation

Global ETS is an electronic testing company, which authenticates electronic devices and is located in Odessa, Florida. They are an ISO 17025 certified and Defense Logistics Agency (DLA) approved laboratory, specializing in authentication process and testing of electronic devices with greater accuracy than other vendors. The company performs Visual Inspection, Decapsulation and X Ray inspection of electronic components in an attempt to ensure that these components are authentic and not counterfeit parts. As a RF/Microwave Intern in Dr. Sadow's group assigned to Global ETS, I got to work on different devices from leading manufacturing companies. I designed test circuit boards using Agilent™ Advanced Design Software and performed RF functionality

tests using a M9372A Pxl Vector Network Analyzer (VNA). The most commonly tested devices were RF transistors, typically used as power and buffer amplifiers in applications like cellular repeater circuits, pre-driver amplifiers in transceiver systems and in Defense systems as signal jammers. In this research a transistor was provided by Global ETS and an amplifier circuit board was designed and fabricated at USF using LPKF ProtoMat S62 and LPKF ProtoMat S63 milling machine. The fabricated board was further tested to verify if the amplifier met the specifications provided by the manufacturer.

3.1.1 RF Amplifiers

Amplifiers are the active electronic devices that increase the voltage, current or power of any input signals. Usually, amplifiers are used in wireless communications, audio equipment, broadcasting and in many wireless applications [3]. Microwave amplifiers are used over a broad range of frequencies [18]. Types of amplifiers usually used in RF applications are:

- Low Noise Amplifiers
- Power Amplifiers
- Linear Signal Amplifiers
- Driver Amplifiers

Low noise Amplifiers are the devices which are used to amplify the low power signals usually received from an antenna without amplifying the noise present in the signals by minimizing additional noise. The role of an LNA is to amplify signals and maintain the signal to noise ratio (SNR) to prevent the loss of information and are used at the initial stage in receiver circuits shown in Figure 14. Since low noise amplifiers are low power consuming devices, they provide voltage gain instead of delivering power to the load [19].

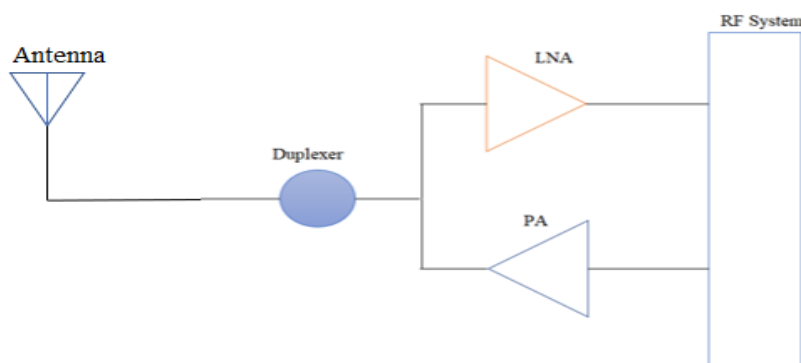


Figure 14: Simple Block Diagram of Transceiver Circuit.

The simple block diagram of a transceiver circuit showing the LNA in the receive signal path (top). The PA is in the transmit path (bottom). The duplexer ensures that the transmit power is isolated from the receiver circuit during receive operation. One of the most commonly used devices in many RF applications to boost the RF signal is a power amplifier (PA). As the name suggests, a power amplifier is an electronic device used to amplify low power radio frequency signals and is typically used in transmitter circuits to drive the transmit antenna. Usually the design specifications include gain, output power, efficiency, P1dB point (Output power at 1dB compression of gain), OIP3 (Output third Intercept Power) and heat dissipation. The PA often includes input and output impedance matching circuits.

Modern power amplifiers operate in different modes to help achieve the desired design goals. These modes are called classes and some of them are Class A, B, AB, C, D, E and F. Usually for RF applications, Class D amplifiers are not chosen due to their tendency to deteriorate efficiency. This usually happens due to the saturated charge storage and finite switching speed of active devices. Many RF amplifiers are made of solid-state devices like bipolar junction transistors, MOSFETs, and MESFETs [18].

Linear signal amplifiers are general amplifiers, referred sometimes as gain block amplifiers, to provide signal gain within the system. These amplifiers do not determine the

dynamic range of a system since they are not located either at the input or at the output of the circuit. Linear signal amplifiers are preferred for their convenience factors such as moderate cost, size and power consumption, which is greater than a low noise amplifier and lesser than a power amplifier and are internally matched. Applications of these amplifiers are significant in industries such as wireless infrastructure, defense, and in transceiver systems to provide internal gain.

Driver amplifiers are used specifically to amplify continuous wave signals at a single frequency and are frequently used in the creation of a local oscillator signal for mixers or in synthesizers. Employing these amplifiers generates maximum performance of the system in electronic warfare, and instrumentation and measurement applications. They are often integrated into CMOS circuits in the transceiver chip in many consumer applications. Efficiency is of greatest concern in driver amplifiers, due to their usage in super heterodyne systems to generate local oscillator signals with power of typically 6 to 10 dB more than the original signal. Due to this, these amplifiers have higher power levels than low noise amplifiers [19].

The applications of each of these amplifiers can be summarized in the following block diagram of the super heterodyne system, which is often used in a radio communication links, radar, imaging systems, satellite and in repeater circuits:

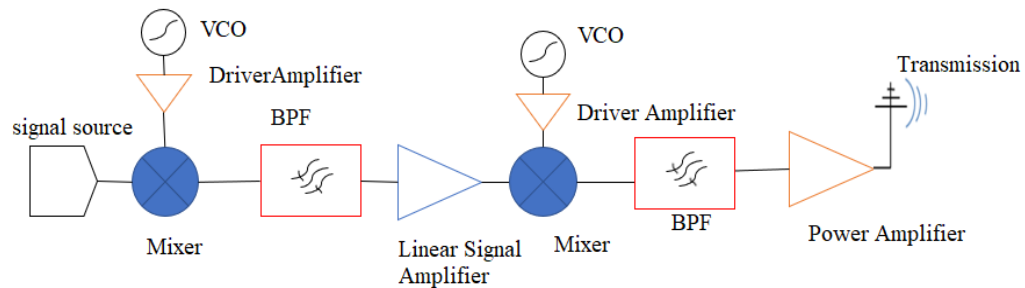


Figure 15: Transmission System Employing Different Amplifier Types as Shown (LNA, PA, Driver, etc.).

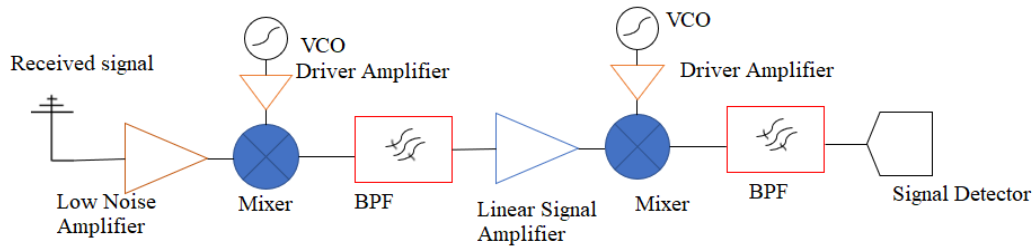


Figure 16: Receiver System Employing Different Amplifier Types as Shown (LNA, PA, Driver, etc.).

The following table summarizes amplifier types and their advantages/Figure of Merit, along with their common applications.

Table 5: Types of Amplifiers and Their Properties

Type of Amplifier	Application	Figure of Merit
Low Noise Amplifier	Amplifying the received signals by antenna	Voltage Gain, Noise Figure, Signal to Noise Ratio (SNR)
Power Amplifier	Amplifying the signals for transmission	Efficiency, linearity
Linear Signal Amplifier	Removing system losses	Gain, Noise Figure and linearity
Driver Amplifier	Generating local Oscillator signals	Phase Noise and Harmonics reduction

3.2 Amplifiers Boards Designed at Global ETS, LLC

3.2.1 Qorvo SGA 3263Z Amplifier

The internship experience at Global ETS, LLC can be summarized as working on three different amplifier boards. One of the boards was designed and fabricated at the company but was

tested using a Vector Network Analyzer (VNA), Spectrum Analyzer (SA) and a Noise Figure (NF) meter at the Center for Wireless and Microwave Information Systems (WAMI) at USF. The transistor, Qorvo SGA 3263Z, was manufactured by Qorvo and is a high performance SiGe Monolithic Microwave Integrated Circuit (MMIC) Amplifier. It acts as a broadband amplifier with a bias supply voltage of 5V. It can be used as a PA Driver amplifier, IF (intermediate frequency) amplifier and has applications in cellular repeater circuits, GSM boost circuits, Wireless Infrastructure, satellite communications, Gain Flatness Compensation circuit and acts a Gain Block Active Bias Circuit in point to point radio communications. The pin-out diagram of this transistor is shown in Figure 17.

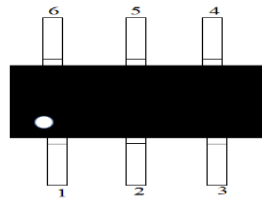


Figure 17: Transistor Pin Diagram of the Qorvo SGA3263Z RF Transistor.

This is an HBT in the Darlington configuration. The SGA 3263Z is a Darlington configuration SiGe (Silicon Germanium) Heterojunction Bipolar Transistor. A Darlington configuration is combination of transistors, which acts as a single transistor with higher current gain (sometimes this is referred to as a ‘super Beta’ transistor [21]. The advantages of using a Darlington pair is with a small base current, a large load can be driven, and heterojunction transistors are popular because of lower leakage currents at the junctions and higher breakdown voltages [3]. The pins 3 and 6 are for RF signal input and RF signal output, and the rest of the pins 1,2,4, and 5 are common ground pins which are grounded. The input signal entered through pin 3 is amplified and collected at the output pin 6. The schematic diagram of this transistor and the fabricated board are shown in Figures 18 and 19. The fabricated amplifier board was then tested,

and the results compared to the parameter specification table from the manufacturers' datasheet in Table 6.

Table 6: Parameter Specifications of SGA 3263Z Amplifier

Parameters	Specification	Units	Condition
Signal Gain	15.0	dB	850 MHz
	13.6	dB	1950 MHz
	13.3	dB	2400 MHz
Output power at 1dB compression	11.6	dBm	850 MHz
	10.9	dBm	1950 MHz
Output Third insertion Point	26.2	dBm	850 MHz
	24.1	dBm	1950 MHz
Bandwidth determined by return losses	5500	MHz	>10 dB
Input return losses	20.3	dB	1950 MHz
Output return losses	21.5	dB	1950 MHz
Noise Figure	3.8	dB	1950 MHz

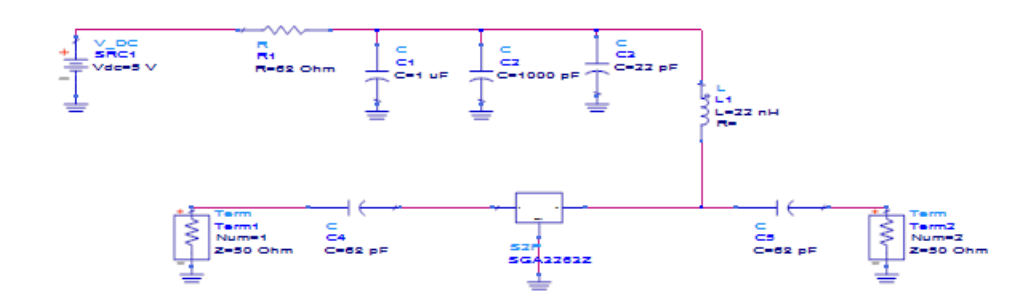


Figure 18: Schematic Diagram of SGA 3263Z Amplifier Board.

The circuit has two DC blocking capacitors at the input and output terminals and a DC feed inductor, known as an RF choke, which blocks RF signals and allows DC signals to pass through it. The bias circuit consists of a 68Ω bias resistor, which was in the datasheet at this voltage and operational frequency. From this schematic design, a layout can be generated, and a PCB can be fabricated to test the transistors as shown in the Figure 19.

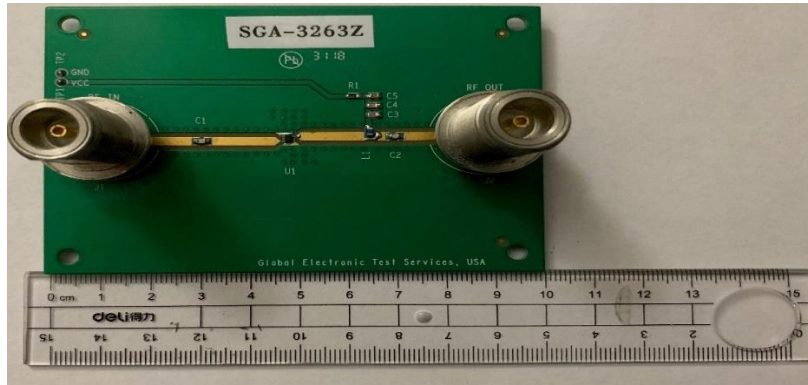


Figure 19: Fabricated PCB of SGA 3263Z from Global ETS, LLC.

The VNA was first calibrated over the frequency range of 300 MHz to 3 GHz using the WAMI calibration kit, called SOLT calibration. Next the Device Under Test, the amplifier board, was placed between the ports of the VNA and the S parameters observed are shown in Figure 20.

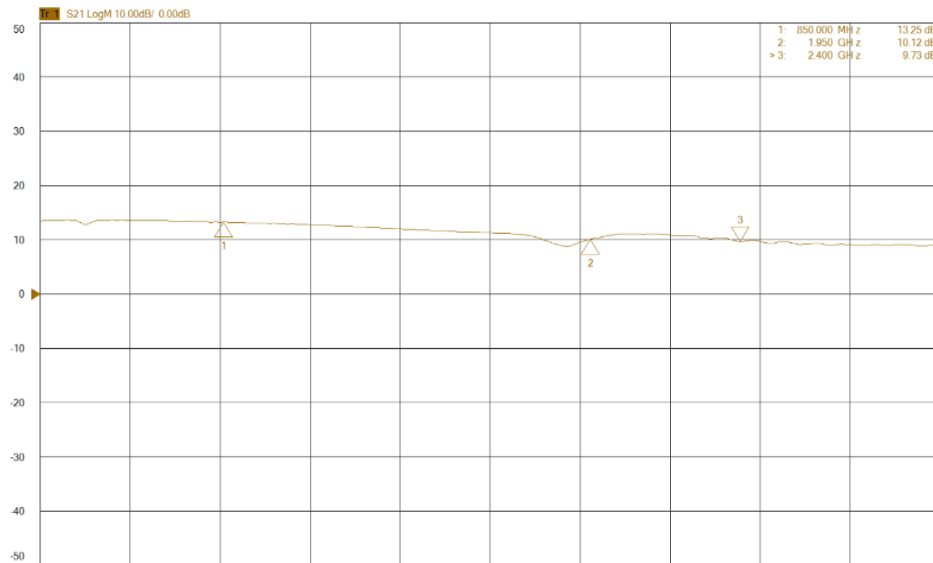


Figure 20a: Gain (S_{21}) dB of the Amplifier Board of Figure 19.

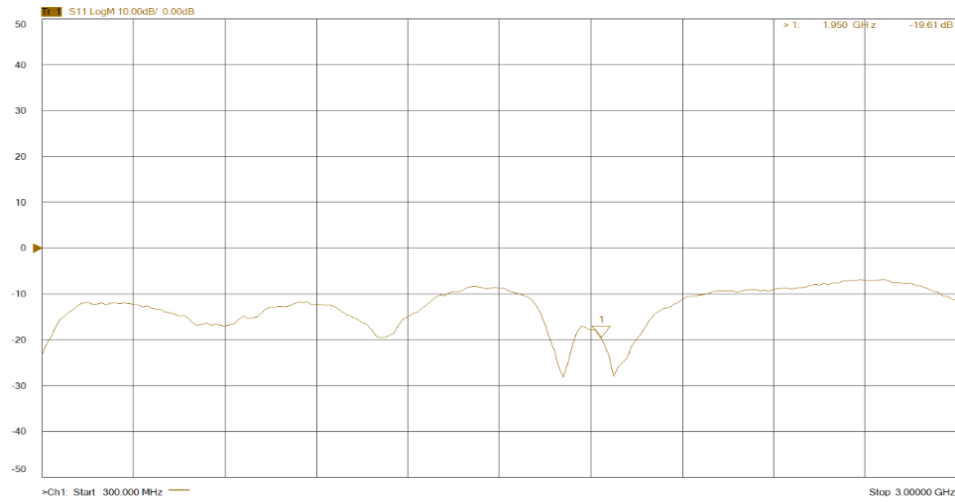


Figure 20b: Input Return Loss (S₁₁) of the Amplifier Board.

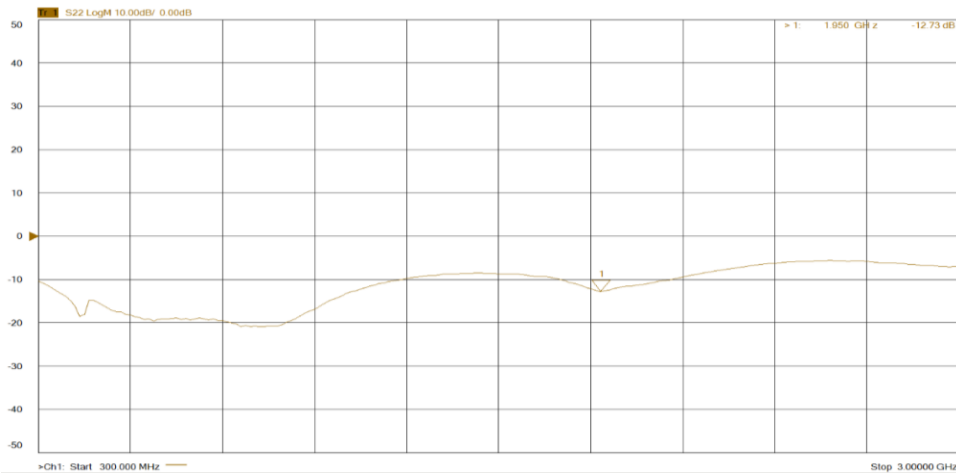


Figure 20c: Output Return Loss (S₂₂) of the Amplifier Board.

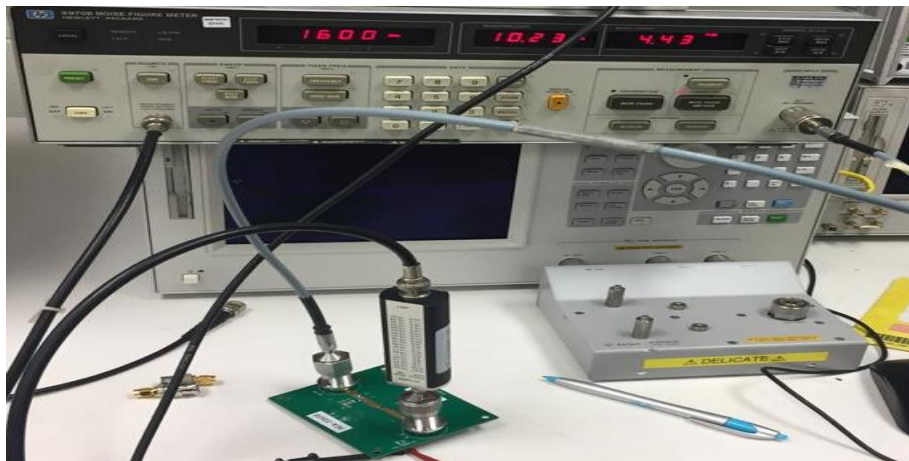


Figure 20d: Noise Figure Measurement Setup of the Amplifier Board.

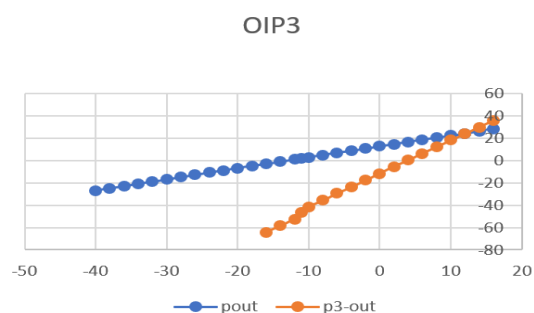


Figure 20e: OIP3 Power at 8520 MHz.

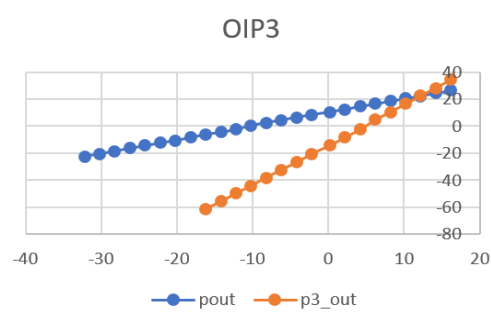


Figure 20f: OIP3 Extrapolated Value at 1950 MHz.

OIP3 is called Output Third Order Intercept Power, which is defined as the output power at which the power of third order components reaches the power level of the fundamental components by extrapolating the curves where the intersection occurs. Hence, OIP3 is a hypothetical point of intersection of power curves of fundamental and third order components. The results are summarized in the Table 7 and compared with the desired specifications.

Table 7: Measured vs Simulated Parameters of SGA 3263Z

Parameters	Measured	Specification	Units	Condition
Signal Gain	13.3	15.0	dB	850 MHz
	10.12	13.6	dB	1950 MHz
	9.73	13.3	dB	2400 MHz
Output Third insertion Point	24.18	26.2	dBm	850 MHz
	22.41	24.1	dBm	1950 MHz
Input return losses	19.61	20.3	dB	1950 MHz
Output return losses	12.73	21.5	dB	1950 MHz

Table 7 continued

Parameters	Measured	Specification	Units	Condition
Noise Figure	4.3	4.1	dB	1950 MHz

We can observe that, at higher frequencies, there is a deviation in the measured results and the desired specifications. This is most likely because of parasitics - since the transistor is internally matched, we did not design any external matching circuits, and this could also impact the measured results.

3.2.2 Qorvo SGA 5586Z Amplifier

The amplifier board was designed for Qorvo's SGA5586Z, which is also a Darlington configuration HBT amplifier. The pinout diagram for the transistor is shown in Figure 21. Since the amplifier is internally matched, matching circuits were not included in the design.

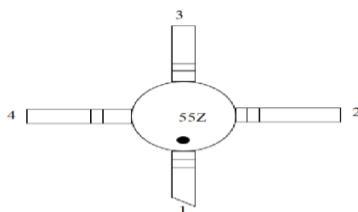


Figure 21: Pin Diagram of SGA5586Z HBT Transistor Darlington Pair.

Pin 1 and 3 are the emitters, pin 4 is the base and pin 2 is the collector of the transistors. The mode of operation is common emitter since the emitter is common to both input and output terminals of the amplifier circuit. The input signal is applied between the base and emitter (ground) and the output signal is measured between the collector and emitter (ground) of the transistor. This configuration is usually preferred because of the high transconductance, or voltage, provided for the given load and is used in many day to day applications of power amplifiers. This circuit consists of a DC block capacitor, DC feed inductor (RF choke) and a bias resistor in a bias circuit.

The amplifier circuit was designed using Agilent™ Advanced Design System software and was simulated with ideal components to compare with the specifications from the manufacturers datasheet, shown in Table 6. Usually, for circuit simulations, we use the Modelithics device library for a specific transistor model. Since this transistor is obsolete, the model was not available in the library. The solution was the an. s2p file which was used to simulate the S parameters of the device at specific bias conditions and frequency. This schematic was simulated to check if the design specifications, such as gain, input return loss, output return loss and noise figure (NF) were met at an operating frequency of 850 MHz. The schematic diagram is shown in the Figure 22 and the simulated S parameters were measured.

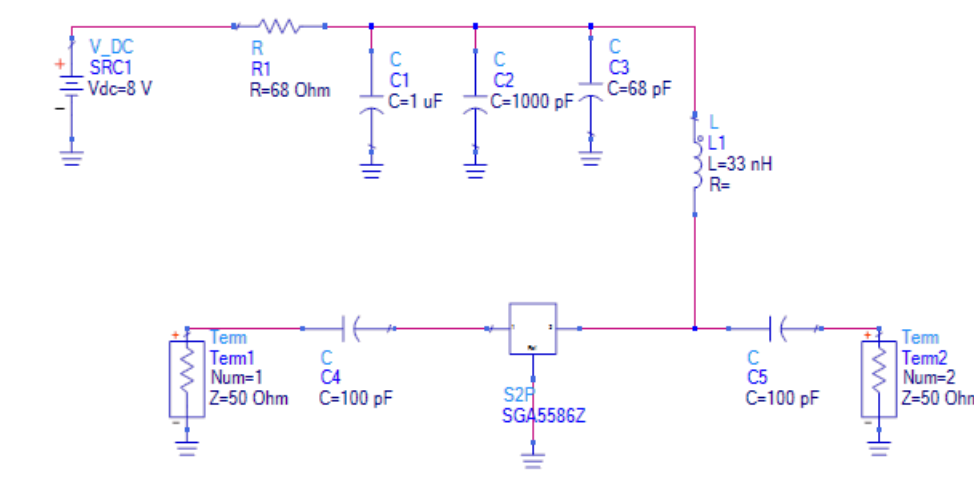


Figure 22: Schematic Diagram of SGA 5586Z Amplifier Board.

Table 8: Desired Specifications Given in Manufacturer's Datasheet

Parameter	Unit	850 MHz
Small Signal Gain	dB	23.1
Input Return Loss	dB	11.8
Output Return loss	dB	18.8

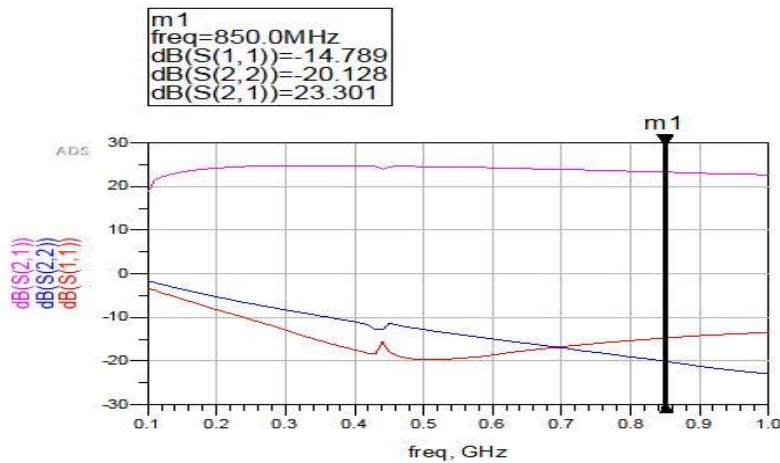


Figure 23: Simulated S-parameters of SGA 5586Z Amplifier Board.

Since this transistor was obsolete we could not fabricate and test the amplifier board. But it can be observed that the simulated parameters and the desired specifications are nearly identical at the operating frequency of 850 MHz. The simulated parameters and the desired parameters were compared in the Table 9

Table 9: Desired Specifications vs Simulated Parameters

Parameter	Unit	Specified Values	Simulated results
Small Signal Gain	dB	23.1	23.301
Input Return Loss	dB	11.8	14.78
Output Return loss	dB	18.8	20.12

3.2.3 Qorvo AG303-86 Amplifier

Buffer amplifiers are responsible for producing isolation between circuit stages usually at the oscillation outputs. Oscillator performance is easily degraded due to poor isolation in the transceiver system. Employing a buffer amplifier can provide better isolation at the output and

improves the noise performance and stability of the oscillator. SOT 363 RFMD AG303-86 is an InGaP Heterojunction Bipolar Transistor (HBT) offering high dynamic range in a low-cost package and is manufactured by Qorvo (previously from TriQuint). It works at different frequency ranges of 500 MHz, 900 MHz and 1.9 GHz. The pin diagram of this transistor is shown in Figure 24.

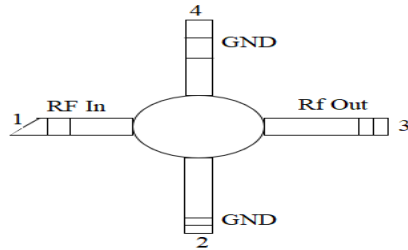


Figure 24: Pin Diagram of AG303-86 Transistor.

Pins 2 and 4 are ground, the RF signal is injected into pin 1 and the RF output signal is observed at pin 3. This amplifier also has a common emitter configuration and the schematic diagram for the amplifier board with DC blocks, RF choke and Bias resistor is shown in Figure 25.

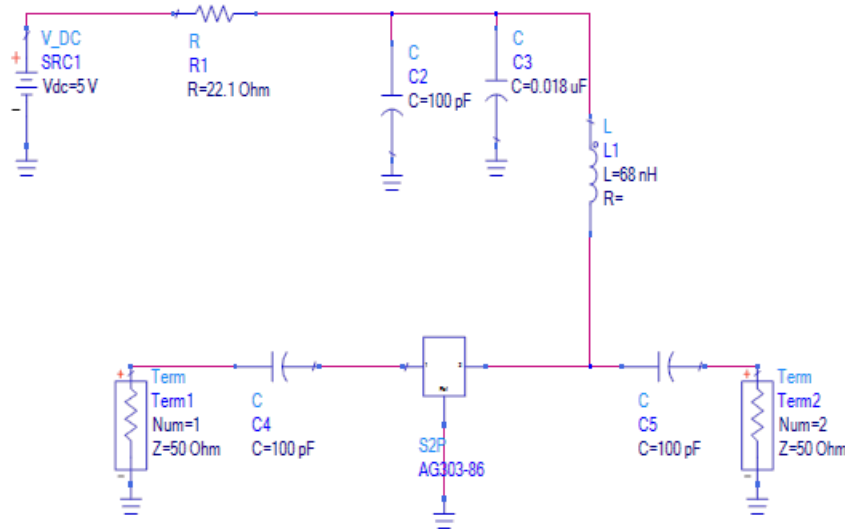


Figure 25: Schematic Diagram of the Amplifier Board.

The schematic diagram has transmission lines and the ideal lumped elements which were replaced with Modelithics elements to consider parasitic effects at the operating frequency. The emitter is grounded using a via and the footprint of the transistor can be drawn according to the manufacturer's datasheet, while the transmission lines were replaced by microstrip transmission lines. The substrate used was FR4. External matching circuits were not designed since the manufacturer's datasheet mentioned that the transistor is matched internally. The quantity of the amplifiers to be tested were more than 6000 so a rapid test method was required. We tested the gain of the amplifier board and utilized a test socket to replace the device under test instead of designing a board and soldering in the transistor package separately for each device. Figure 26 shows one of the test sockets for testing an amplifier board.

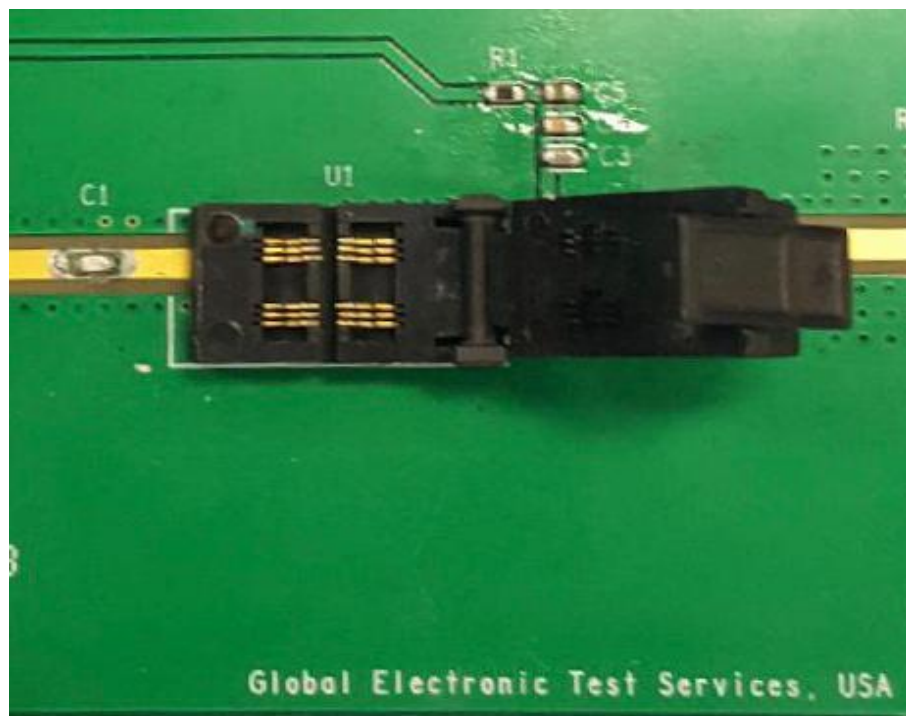


Figure 26: RF Test Socket on the PCB to Test Each of 6000 RFMD AG303-86 InGaP HBTs.

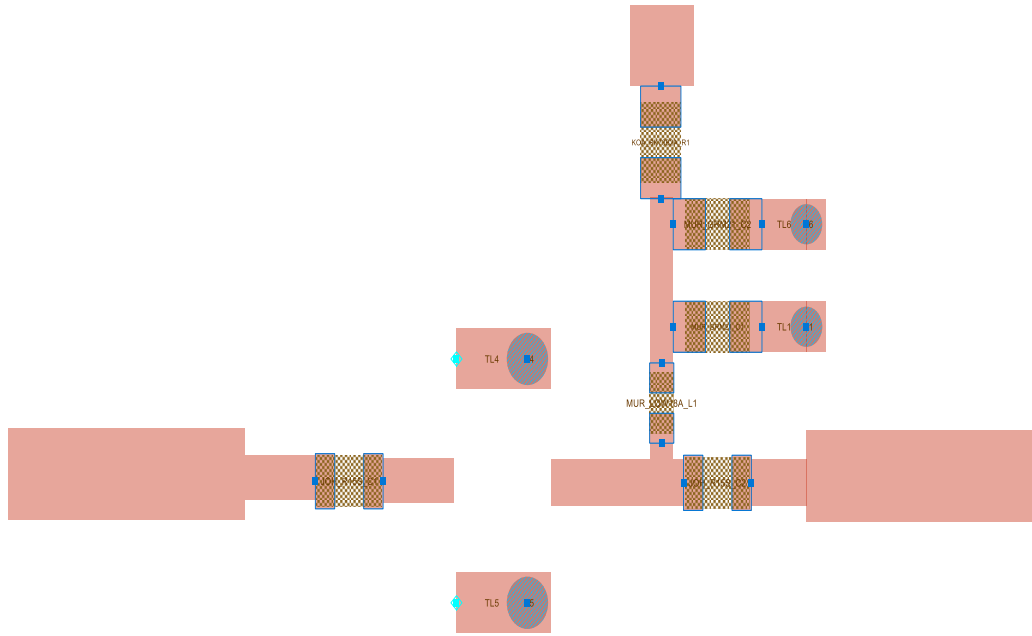


Figure 27: Layout of AG303-86G Amplifier Board.

We did not have the Modelithics model of the transistor, only the mechanical footprint drawing information from the datasheet. The foot prints of the lumped elements are due to the components from the Modelithics library, which consider the parasitic effects at the operating frequency. The assembled board for testing is shown in Figure 28.

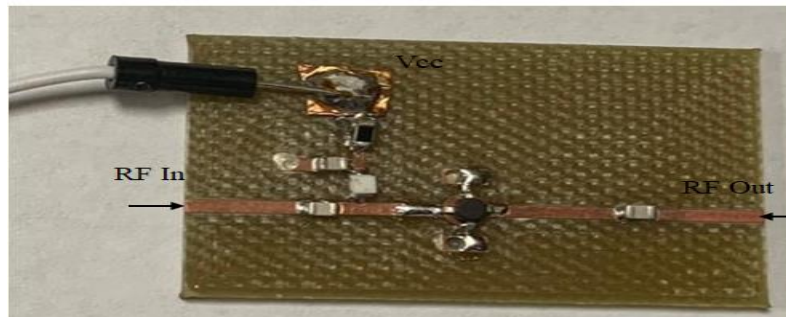


Figure 28: Assembled Board of the Amplifier Containing the TriQuint AG303-86.

The fabricated board was milled with an LPKF ProtoMat S63 using FR4 as the substrate and the lumped elements were assembled. This board was later tested using a Vector Network Analyzer after performing SOLT (short-Open-Load-Thru) calibration. This calibration is usually

performed to shift the reference plane from the ports of VNA to the Device Under Test (DUT) ports. The gain was measured by observing S_{21} at the operating frequency, shown in Figure 29.

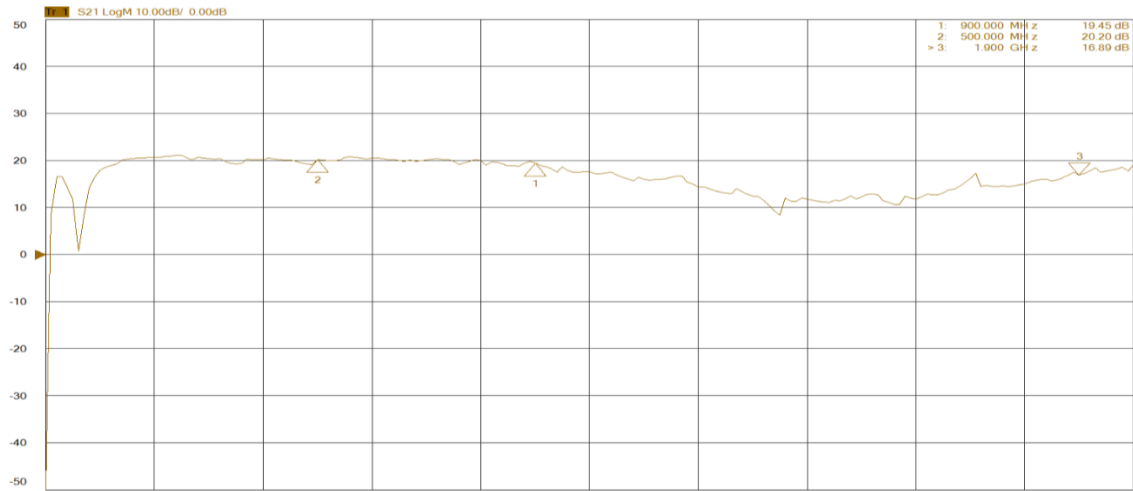


Figure 29: Measured Gain of the TriQuint AG303-86G InGaP HBT Amplifier Board from 300 MHz to 2 GHz.

It is observed that the measured gain was equal and meets the desired gain at the operating frequency. The gain of the amplifier at 900 MHz, 500 MHz and 1.9 GHz was 19.45 dB, 20.20 dB and 16.89 dB, respectively, which meets the desired conditions. The Table 10 shows the desired and measured parameters at different frequencies.

Table 10: Gain (dB) vs Frequencies (MHz) AG303-86 Amplifier

Frequency	Gain (dB)
500 MHz	20.20
900 MHz	19.45
1.9 GHz	16.89

CHAPTER 4

DESIGN AND FABRICATION

In the field of Microwave and RF devices, power dividers are typically passive devices which couple power in the form of electromagnetic waves from one port allowing the signal to be used in other ports or circuits. Wilkinson's power divider helps in achieving isolation between the load ports while maintaining matched conditions at all the ports. Since the power divider is a passive device, it can also act as a power combiner due to the reciprocal properties of the device. The design, construction and simulation results are discussed in this chapter.

4.1 Microstrip Transmission Lines and Dimensions

Microstrip lines are often used to build active and passive circuit boards since fabrication techniques like milling and photolithography are easily adopted. Microstrip technology is compact and economical when compared to waveguide technology. It has a dielectric layer called the substrate which separates the conductive signal layer from a metal ground plane. The microstrip layout with conductor width W , substrate thickness H and substrate permittivity ϵ_r [13] is shown in Figure 30. The disadvantages of using microstrip transmission lines are that they are unable to handle high frequency signals, have lower power handling capacity and more losses than hollow-pipe metal waveguides. Microstrip lines exhibit interference between traces due to signal radiation and cross talk since they are not enclosed like waveguides. FR4 and Alumina are the most commonly used dielectrics [22] used at these frequencies.

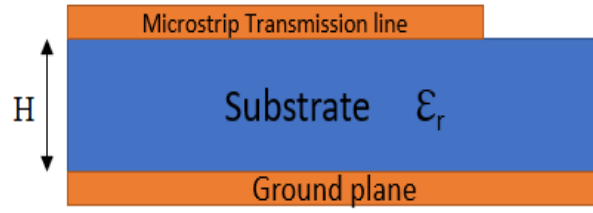


Figure 30: Microstrip Transmission Line on a Substrate with Relative Permittivity ϵ_r .

Since the dielectric separates signal line and ground plane, the absence of the substrate implies the presence of air, which leads to the TEM mode of propagation (transverse electromagnetic mode). Due to the non-ideal dielectric between the conductor (microstrip line) and the ground plane, a perfect TEM mode of propagation is not possible for microstrip lines [13]. When the wavelength is longer than the substrate thickness, the so-called quasi TEM mode of propagation is observed, which is very close to the true TEM mode. While designing a microstrip line, properties like width of conductor (W), propagation constant (β), phase velocity (v_p) and wavelength (λ) are considered and related by the formula (4.1)

$$V_p = \frac{\lambda}{T} \quad (4.1)$$

$$= \frac{c}{\sqrt{\epsilon_{eff}}} \quad (4.2)$$

$$\beta = k\sqrt{\epsilon_{eff}} \quad (4.3)$$

where K is the propagation constant of free space ($k = \omega\sqrt{\mu_0 * \epsilon_{eff}}$), C is the speed of light ($3*10^8$ m/s) and ϵ_{eff} is the effective dielectric constant of the substrate and air, which is a function of relative permittivity of the substrate, width of the conductor and thickness of the substrate. The relation between the wavelength (λ) of the microstrip line and the phase velocity is given by (4.4)

$$\lambda = \frac{c}{f*\sqrt{\epsilon_{eff}}} \quad (4.4)$$

where f is the operating frequency of the device in Hertz (Hz).

The characteristic impedance of a microstrip device also depend on the width of the conductor and the dielectric thickness. Since Wilkinson's power divider employs quarter wavelength transmission lines, lengths and widths of these lines depends on the chosen substrate and conductor thickness and are calculated using the Linecalc™ tool from Advanced Design System (ADS™) software.

4.2 Ideal Design of Wilkinson Power Divider and Expected Performance

As discussed, Wilkinson's power divider has input and output port impedances of 50Ω and 70.71Ω for quarter wavelength transmission line elements. These calculations were made easy by employing Linecalc tool and substituting the parameters of a chosen 59 mil thick FR4 substrate at an operating frequency of 2.4 GHz. There is a resistor between the output ports with a resistance of $2*Z_0$, where Z_0 is the characteristic impedance (50Ω) in this circuit. Table 11 has information about the substrate and specifications being used in an ideal power divider design.

Table 11: Specifications and Values of the Chosen FR4 Substrate

Specification	Value (unit)
Relative Dielectric constant	4.3
Substrate thickness	1.58 mm
Conductor thickness	0.035 mm
Dielectric loss Tangent	0.022
Frequency of operation	2.4 GHz

The resulting dimensions computed by Linecalc are as follows for a 50Ω transmission line: width of 3.0327 mm, length of 17.2212 mm and for the 70.71Ω quarter wave transmission line

elements the lengths and width are 1.5839 mm and width is 17.7236 mm, respectively. The circuit schematic for the design is shown in the Figure 31.

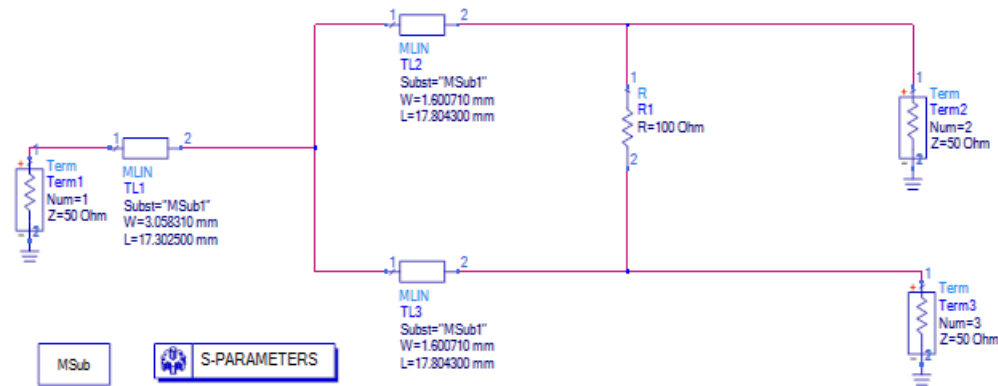


Figure 31: Ideal Schematic Circuit of Wilkinson's Power Divider to be Fabricated on FR4 Substrate Board.

The S-parameters of the simulated circuit at a center frequency of 2.4 GHz were simulated. The predicted input and output return losses (S_{11} , S_{22}) exceeded 40 dB and the isolation between the output ports was ~ 45 dB. The insertion losses were approximately equal to 3dB, as expected (half-power split of input (i.e., Port 1) injected power). The simulated results are shown in Figure 32.

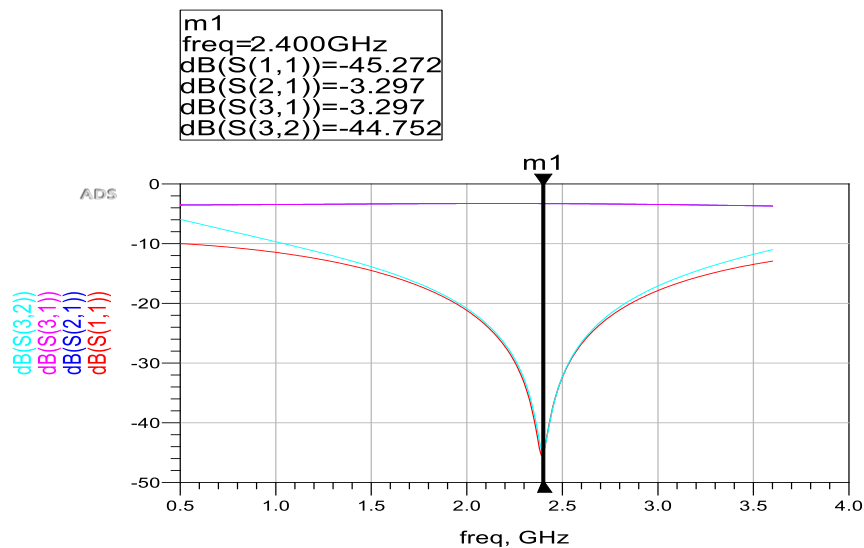


Figure 32: Simulated Results of Wilkinson's Power Divider Using the Circuit Design.

The device parameters observed were bandwidth, input return loss (S_{11}), output return loss (S_{22} and S_{33}), isolation between output ports, power division or amplitude balance and phase balance. Typically, manufactured power dividers available in the market were able to achieve 65:1 of bandwidth [16] with multiple quarter wavelength transmission line sections and a VSWR of 1.3:1 for input return losses greater than 15 dB and the VSWR of 13.48 dB [15]. Isolation is also an important factor and values greater than 15 dB provide good isolation between the output ports across the specified bandwidth. Depending upon the bandwidth of the device, the amplitude balance is usually ± 0.45 dB (difference in insertion losses). These values were observed for the power dividers manufactured by the companies in the market. The results expected are summarized in the Table 12.

Table 12: Commercial Wilkinson's Power Divider Specifications [15]

Parameter	Expected results
Isolation between output ports	> 15dB
Output Port Amplitude Balance	± 0.2 dB
Return Losses	>15 dB

4.3 Design and Simulated Results of Wilkinson's Power Divider

Since Wilkinson's divider has many design topologies, different microstrip junctions were designed and constructed with an operating at a frequency of 2.4 GHz. ADS™ software was used for the designs. Circuit CAM 4.0™ and LPKF Circuit Board plotter™ software were used to fabricate the power dividers. The results were observed using a Keysight PXIe Vector Network analyzer™.

4.3.1 Design and Construction of Curved Wilkinson Divider with Step Junction

As the name indicates, the design has a step junction between the quarter wavelength transmission lines and 50Ω terminations at the output ports. The schematic is shown in the Figure 33.

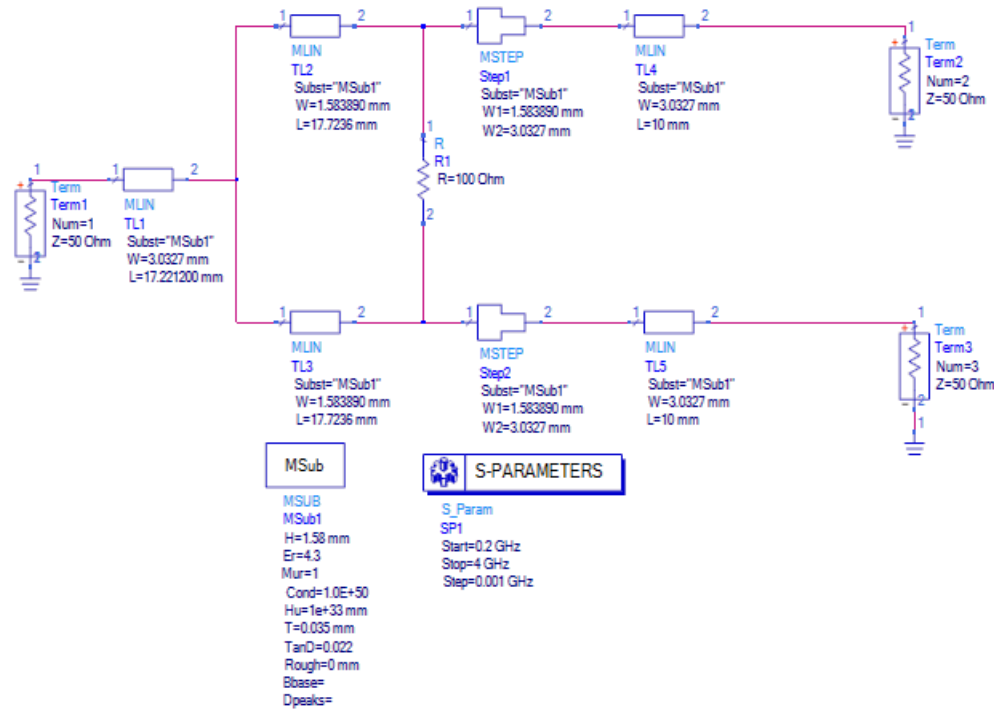


Figure 33: Schematic Diagram of Curved Power Divider with Step Junction.

The step junction connects the conductor of width W_1 (mm) at pin 1 to the conductor of width W_2 (mm) at pin 2. Usually a step junction is employed when two transmission lines of different widths are connected in a circuit. The layout of this divider can be generated from the schematic using Generate/update Layout tool in ADSTM. The above schematic is simulated and the parameters such as input and output return losses, isolation between the ports, insertion losses observed are shown in Figure 34. To include the parasitic effects, a Modelithics (Tampa, FL) resistor was used in the design between the output ports to provide isolation.

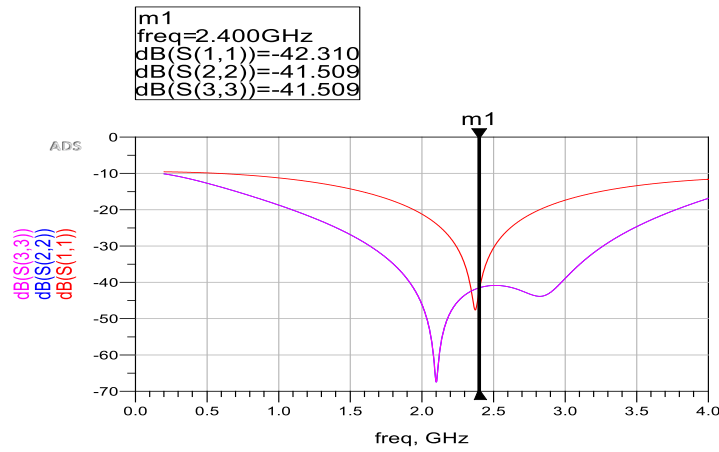


Figure 34a: Simulated Input Return Loss (S_{11}) and Output Return Loss (S_{22} , S_{33}) in dB of Design 1.

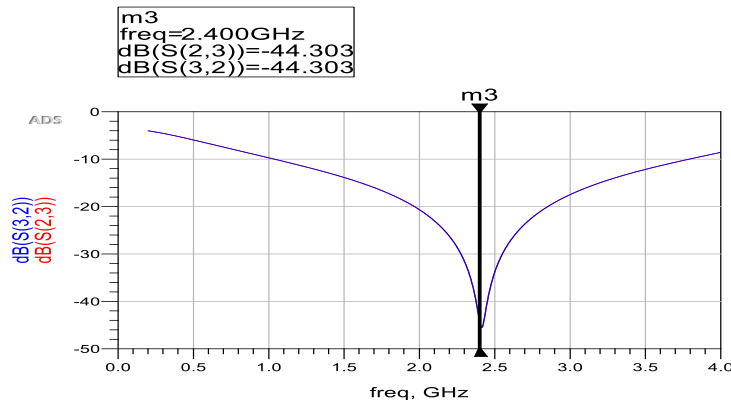


Figure 34b: Simulated Isolation between the Output Ports 2 and 3 (S_{32} , S_{23}) in dB vs F (GHz) of Design 1.

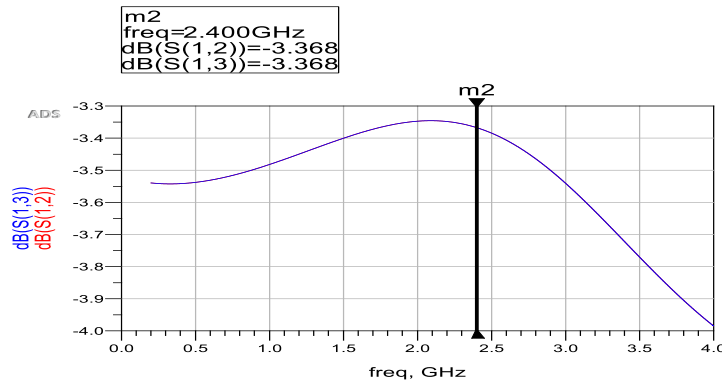


Figure 34c: Simulated Insertion Losses (S_{21} , S_{31}) in dB vs F (GHz) of Design 1.

It was observed that the input return losses and output return losses were greater than 40 dB, indicating more than 99.9% of the power was transferred. The device operates with better amplitude balance within the frequency range of 1.63 - 3.21 GHz, with a center frequency of 2.28 GHz and providing the bandwidth of 70%. Bandwidth can be calculated by observing the lower and higher frequencies of operation using the formula 4.5

$$BW = \frac{F_H - F_L}{F_c} * 100\% \quad (4.5)$$

$$F_c = \sqrt{F_L * F_H} \quad (4.6)$$

where F_L is the lowest frequency ($F_L = 1.632\text{GHz}$), F_H is the highest frequency ($F_H = 3.213\text{GHz}$) and the center frequency (F_c) was 2.28 GHz. The values of insertion losses were the same and hence the power was divided equally. The isolation between the output is greater than 40 dB, indicating that the output ports are isolated while the input port is matched to a 50Ω load.

4.3.2 Wilkinson Divider with Continuous Taper

This design is similar to the above design of the divider but has a continuous taper instead of a microstrip step junction. The taper connects the transmission lines of different widths and induces additional length to describe the widths of the transmission lines. The difference between a microstrip step and tapered junctions are primarily observed in the design layout. The schematic design of the divider circuit with tapered junction is shown in Figure 35. The length of the quarter wave transmission line for this design was 17.0236 mm due to the tapered length of 0.7 mm.

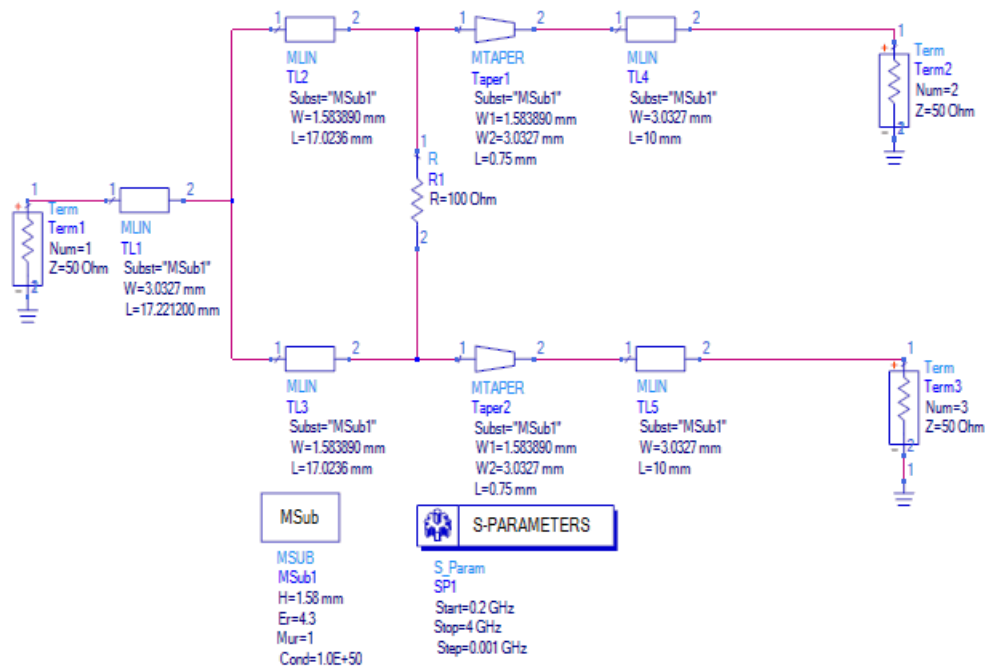


Figure 35: Schematic Diagram of a Power Divider Circuit with Tapered Junction Between the 50Ω and 70.71 Ω Transmission Lines.

The above circuit is simulated over the range of 0.2- 4.0 GHz and the observed simulated results are shown in the Figure 36.

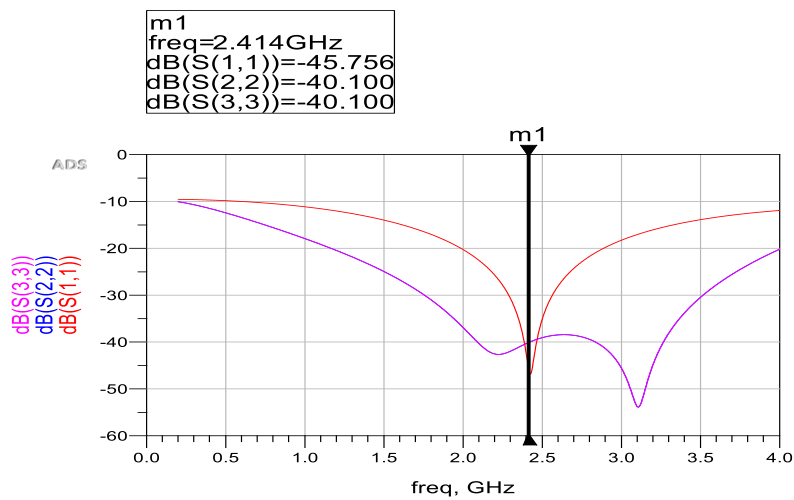


Figure 36a: Simulated Input and Output Return Losses (S_{11} , S_{22} and S_{33}) in dB of Design 2.

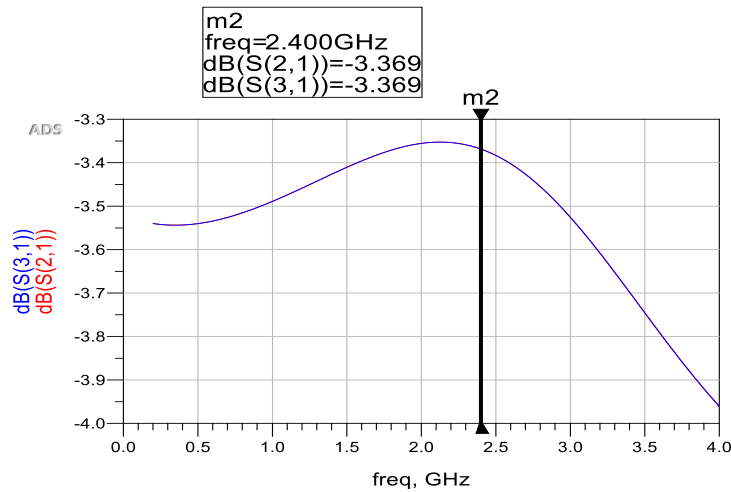


Figure 36b: Simulated Insertion Losses (S_{12} , S_{13}) in dB of Design 2.

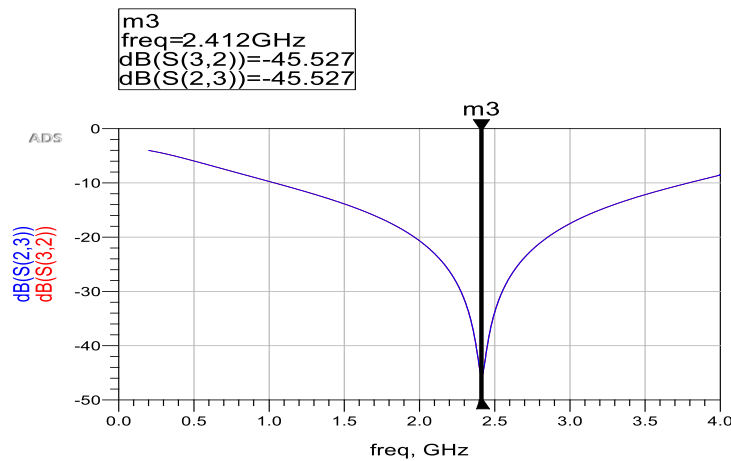


Figure 36c: Simulated Isolation between the Output Ports in dB (S_{32} , S_{23}) of Design 2.

The predicted input return losses and output return losses were greater than 40 dB indicating 99.9% of transmitted power. The insertion losses were approximately the same representing equal power division between the output ports from the input port from Figure 37b. The isolation of the device also plays a major role since Wilkinson's dividers are known for matched ports while isolating the output ports at operating frequency. The simulated results observed were greater than 40 dB indicating better isolation between the ports. The maximum performance is in the frequency range of 1.66 - 3.25 GHz with a bandwidth of 70% approximately. Phase balance between the output ports is also an important parameter to be noted while designing

a power divider. It was also observed that the power at the output ports was also in phase and the power delivered at the output ports is equal to half the power at input port.

4.3.3 Wilkinson's Divider Design using Co-simulation

This power divider was designed using a method called Co-simulation. This method allows one to design parts of the circuit for simulation. Initially, a layout with proper dimensions is designed and then a symbol is generated, which is later added into the circuit schematic for simulation in the desired frequency range. This method is advantageous since an EM (Electromagnetic) simulation is performed which, in principle, is more accurate than an idealized circuit simulation. The circuit schematic was also designed to show the comparison between the different design topologies and is shown in Figure 37 with the layout in Figure 38.

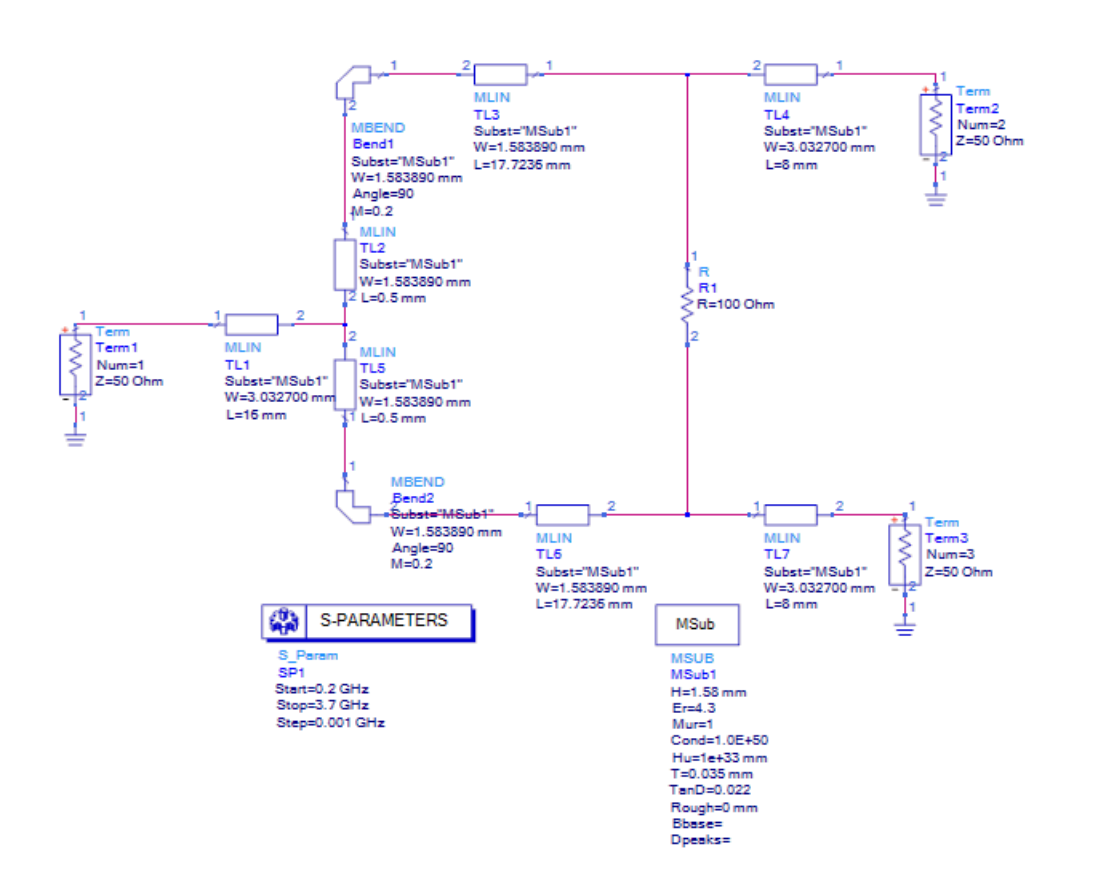


Figure 37: Circuit Schematic of Straight Power Divider.

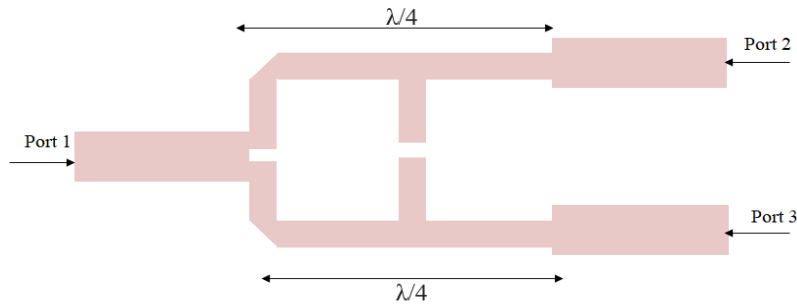


Figure 38: Layout of Straight Power Divider Using Co-simulation Method.

EM simulation was performed by assigning a substrate (FR4) (Fig. 39), with dielectric constant, conductor and substrate thicknesses from Table 12. An EM simulation was performed, and a symbol generated to measure the isolation after adding the output resistor. Terminations and a KOA 100Ω resistor were added to the symbol, as shown in Figure 40, to perform the circuit simulations.

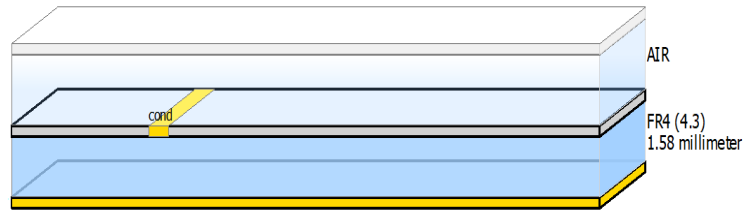


Figure 39: Substrate Dimensions for Performing EM Simulation on Straight Power Divider.

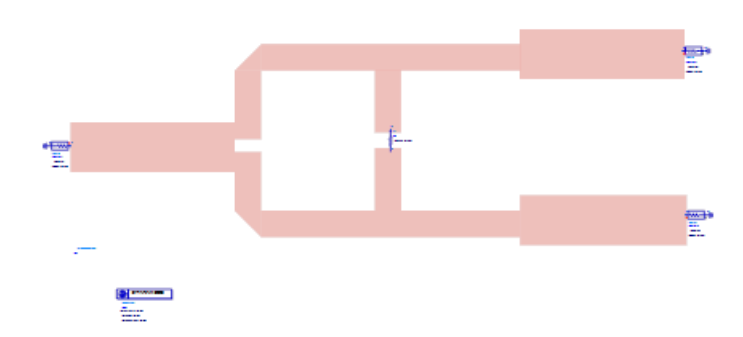


Figure 40: Circuit Layout Created Using Co-sim Method Using the Straight Power Divider Symbol.

The following S parameters were predicted after performing circuit simulations in the frequency range of 300 MHz to 4 GHz.

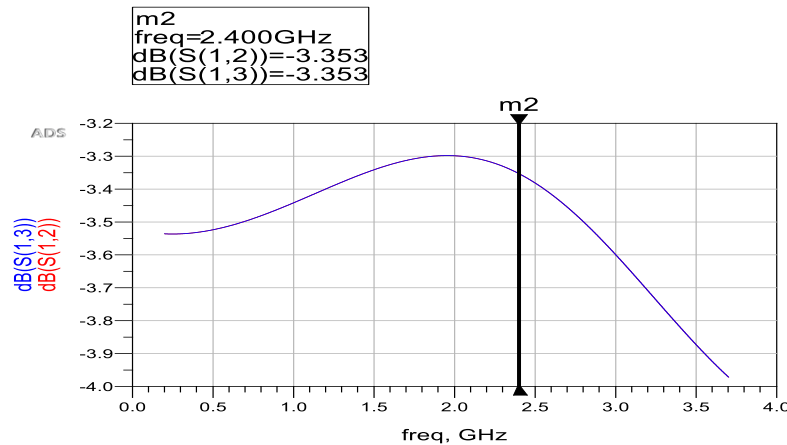


Figure 41a: Insertion Losses in dB vs. F (GHz) of Design 3.

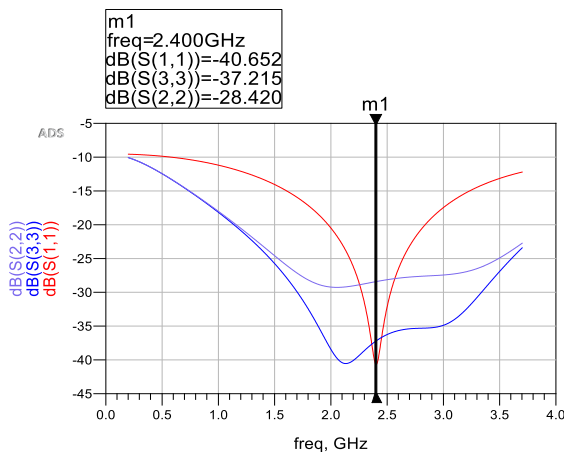


Figure 41b: Simulated Design 3 Input and Output Return Losses.

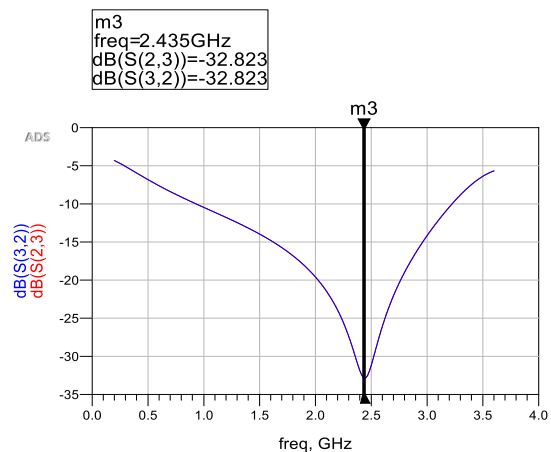


Figure 41c: Simulated Design 3 Isolation.

From the above simulated data, it was observed that the input return losses were 40 dB indicating that maximum power should be transferred, and output return losses were above 25 dB indicating less than 0.1% of power was reflected. The insertion losses were equal indicating equal power division. The isolation between the output ports was maximum at a frequency of 2.435 GHz. These updated layouts were fabricated using the LPKF Protomat S62 milling machine.

4.3.4 Layouts of Power Divider Circuits

The layouts of power dividers designed using ADS is shown in Figures 42 a, b and c

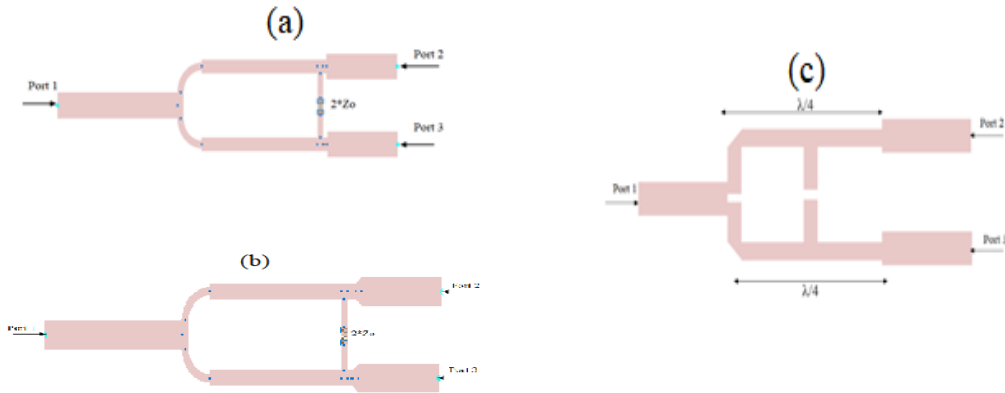


Figure 42a, b: Step and Tapered Junction

Figure 42c: Straight Power Divider.

Power Dividers.

The quarter wavelength microstrip transmission lines have a common length of 17.73 mm after optimizing the circuit to meet the specifications. The quarter wavelength transmission lines were separated by 1 cm, which affects the performance of the divider due to coupling between the transmission lines. Isolation is primarily affected by coupling across the gap between the transmission lines.

4.4 Construction and Results

The divider boards were fabricated using LPKF S62 Protomat milling machine. Initially the .dxf/dwg file was generated by the ADSTTM software and then imported into the CircuitCAM software for the machine to assign the excess copper and copper conductor traces and then exported the file to LMD extension for the fabrication process. This file was later imported in the Board Plotter software to guide the milling process manually step-by-step by adjusting the placement of the design on the substrate board for fabrication. The fabricated boards are shown in Figure 43a, b and c.



Figure 43: Photographs of the Milled Wilkinson Power Dividers with (a) Step Junction, (b) Taper Junction and (c) Straight Dividers.

The S parameters of the constructed boards were measured using a Keysight PXIe Chassis Vector Network Analyzer. The VNA was calibrated initially to shift the reference plane to the tip of the coaxial cables where the Device Under Test (DUT) is tested in the frequency range of 300 KHz to 4 GHz. The measured results are shown in the Figures 44, 45 and 46.

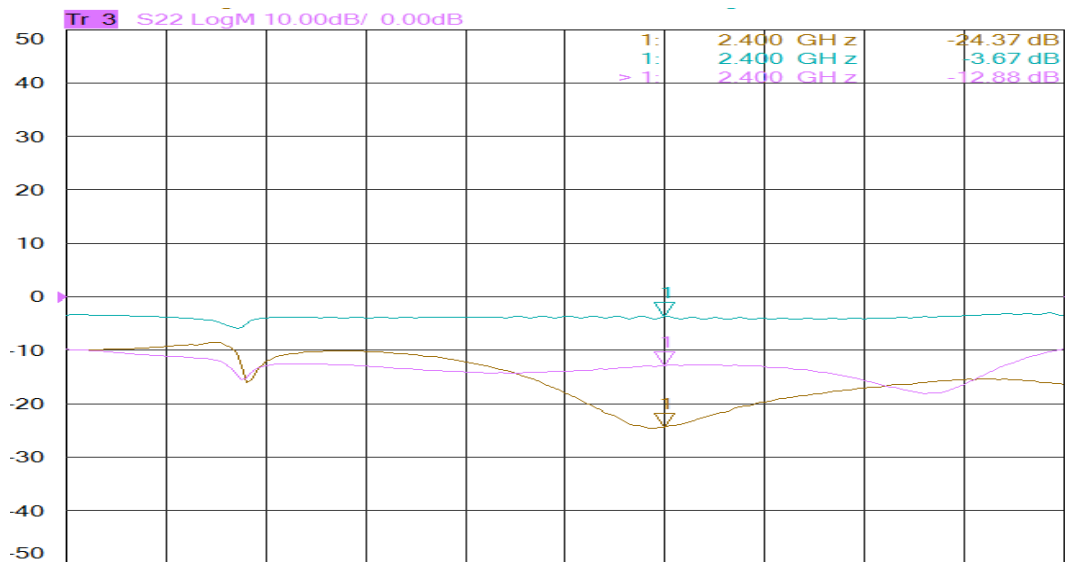


Figure 44a: Input Return Loss (S_{11}), Output Return Loss of Port 2 (S_{22}) and Insertion Loss of Port 2 (S_{21}) vs. F (GHz) of Design 1.



Figure 44b: Insertion Loss of Port 3 (S_{31}) vs. F (GHz) of Design 1.

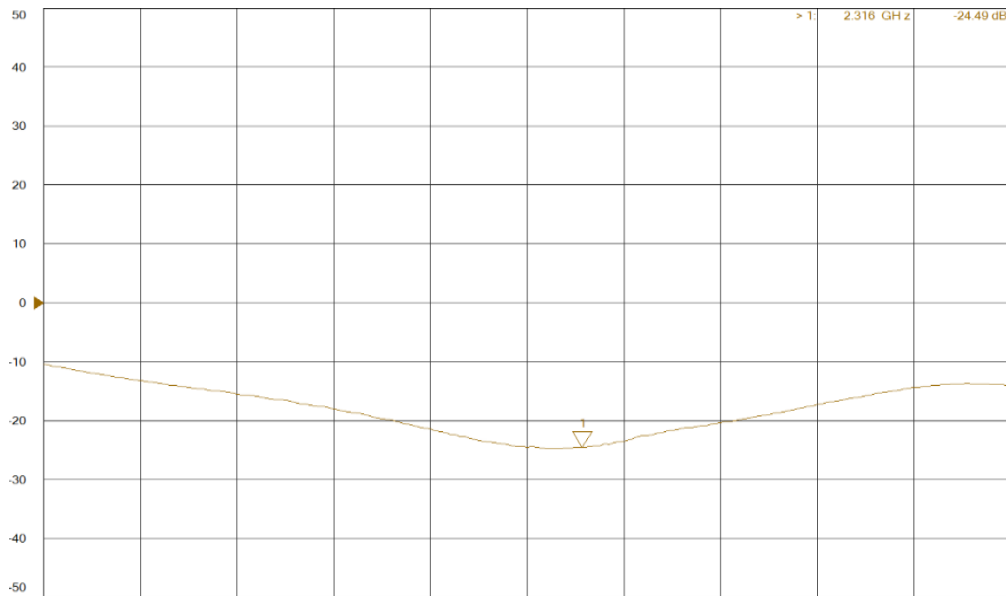


Figure 44c: Output Return Loss of Port 3 (S_{33}) vs. F (GHz) of Design 1.

Input and output return losses were greater than 15 dB within the frequency range of 1.67 - 2.35 GHz resulting in a power transfer of 95% and the maximum output Port 3 return loss was observed at 2.316 GHz, which is approximately equal to the simulated return losses of the step design at 2.40 GHz. The insertion losses at Port 2 and Port 3 were 3.67 dB and 3.774 dB, respectively, which were closer to the simulated results at 2.4 GHz. The difference between the

insertion losses of Ports 2 and 3 is called the Amplitude Balance and was observed as 0.07 dB, indicating power division was almost equal between the output ports.

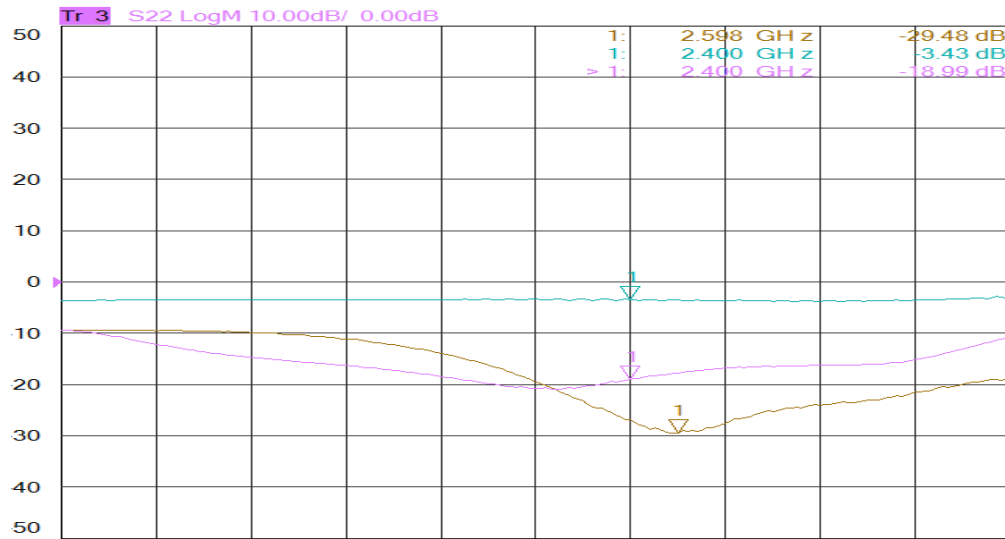


Figure 45a: Input Return Loss (S_{11}), Output Return Loss of Port 2 (S_{22}) and Insertion Loss of Port 2 (S_{21}) vs. F (GHz) of Design 2.

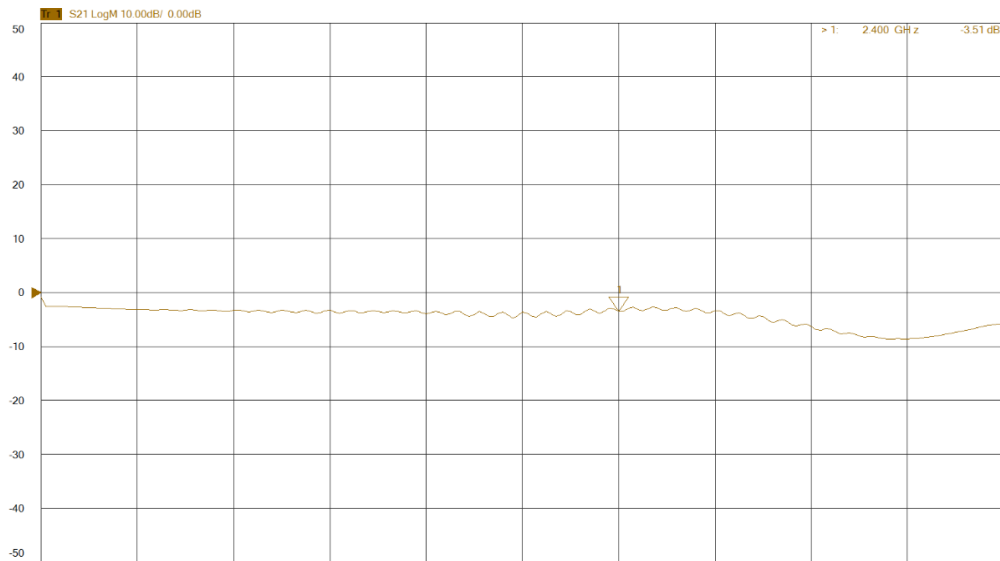


Figure 45b: Insertion Loss of Port 3 (S_{31}) vs. F (GHz) of Design 2.

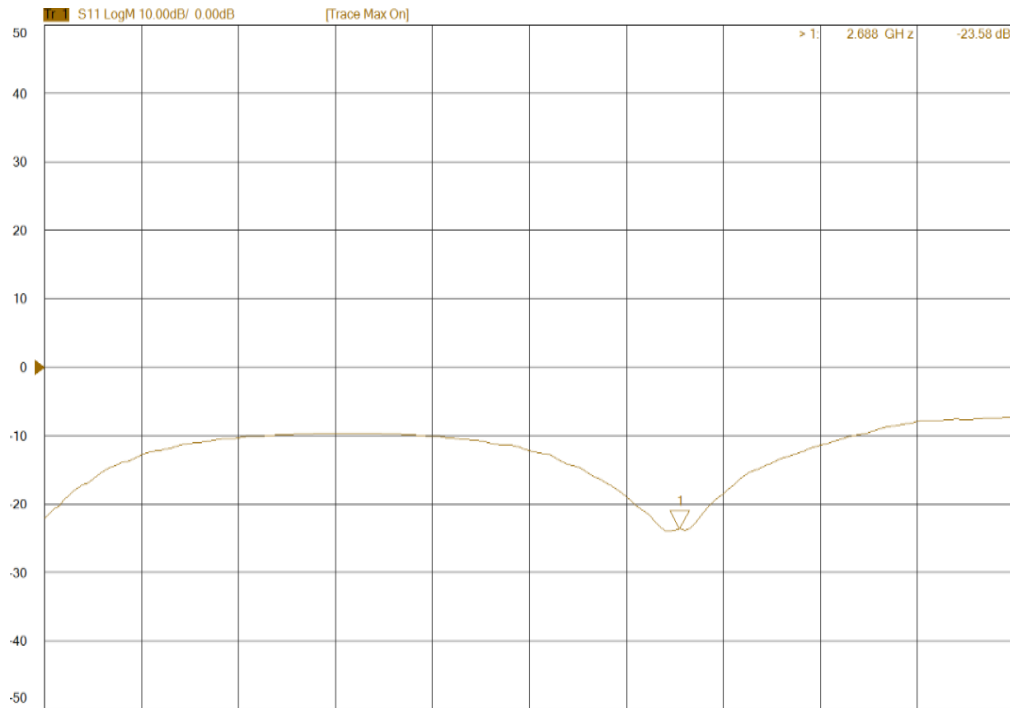


Figure 45c: Output Return Loss of Port 3 (S_{33}) vs. F (GHz) of Design 2.

The tapered junction power divider was measured by following the same calibration process. The input return losses (S_{11}) were almost 30 dB at a frequency of 2.598 GHz and the output return losses (S_{22} and S_{33}) were greater than 15 dB between the frequency range of 1.68 - 3.12 GHz and were maximum at 2.4 GHz and 2.78 GHz, respectively. This indicated the maximum percentage of power transfer between the ports. The measured insertion losses were 3.43 dB and 3.51 dB for Ports 2 and 3 with an amplitude balance of 0.08 dB. This indicates that the power division was effective. The insertion losses were better for the tapered divider compared to the step divider. However, the step divider had better performance in terms of return loss at the operating frequency since there was a frequency shift due to losses in this model.

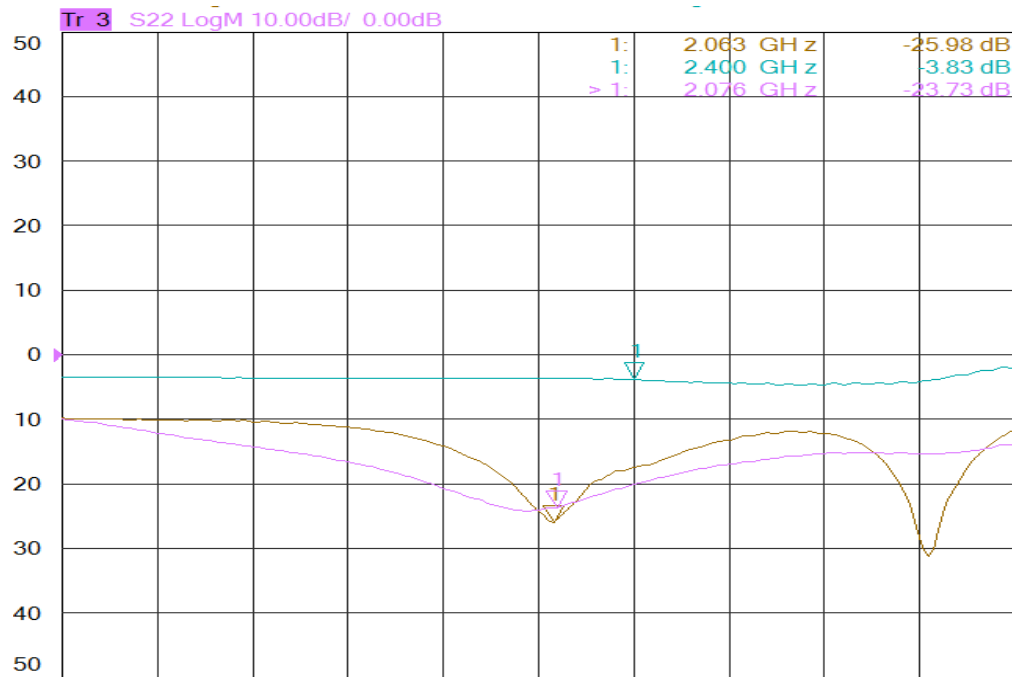


Figure 46a: Input Return Loss (S_{11}), Output Return Loss (S_{22}) and Insertion Loss (S_{21}) vs. F (GHz) of Design 3.

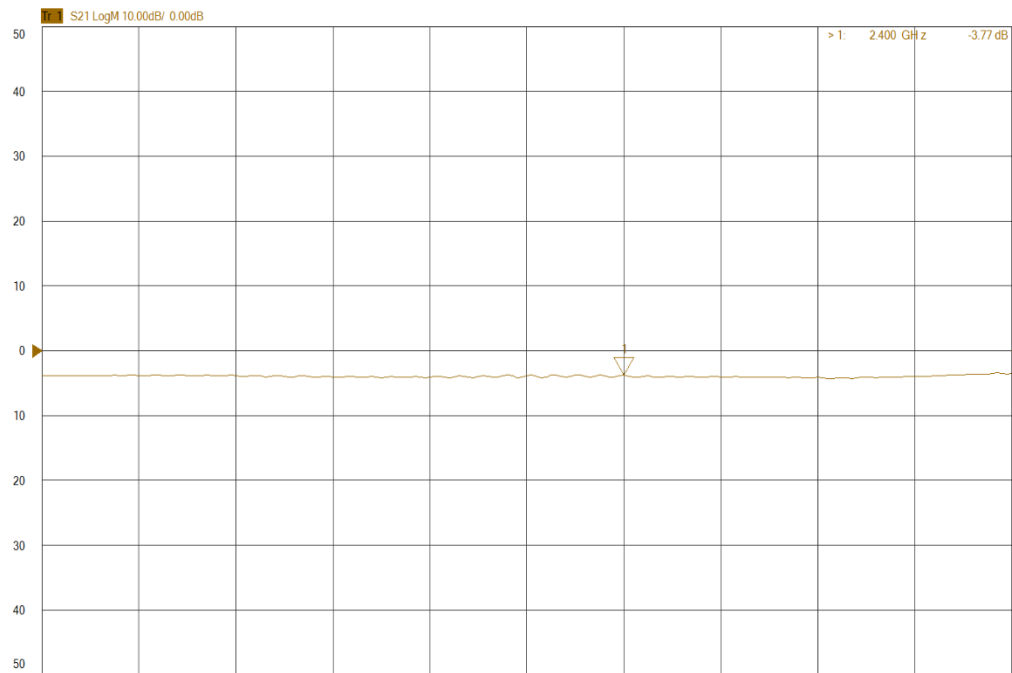


Figure 46b: Insertion Loss of Port 3 (S_{31}) vs. F (GHz) of Design 3.

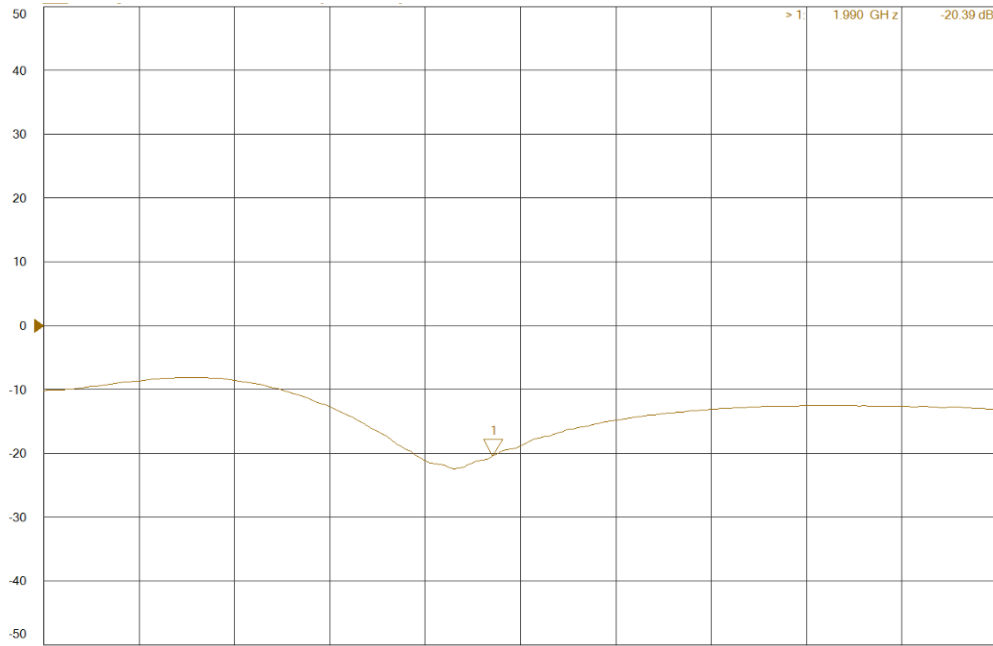


Figure 46c: Output Return Loss of Port 3 (S_{33}) vs F (GHz) of Design 3.

The input return losses were greater than 20dB indicating more than 98% of the power is transferred to the output ports and the output return losses were greater than 15 dB indicating 95% of power transfer at 2.07 GHz and 1.9 GHz for the measured straight divider. The insertion losses of Ports 2 and 3 were 3.83 dB and 3.77 dB, respectively, which was equal to the simulated value and the amplitude balance was 0.06 dB. The measured results of the straight divider were similar to the step divider although the tapered divider had better results when compared to these dividers. It can also be observed that the frequency range where the input and output return losses were maximum was approximately the same for each design and were greater than 15 dB and the insertion losses were in the range of 3.3 dB to 3.8 dB assuring that the power division between the input and output ports was approximately half. The isolation between the output ports is shown in Figure 45 for the step junction, tapered junction curved divider and straight divider.

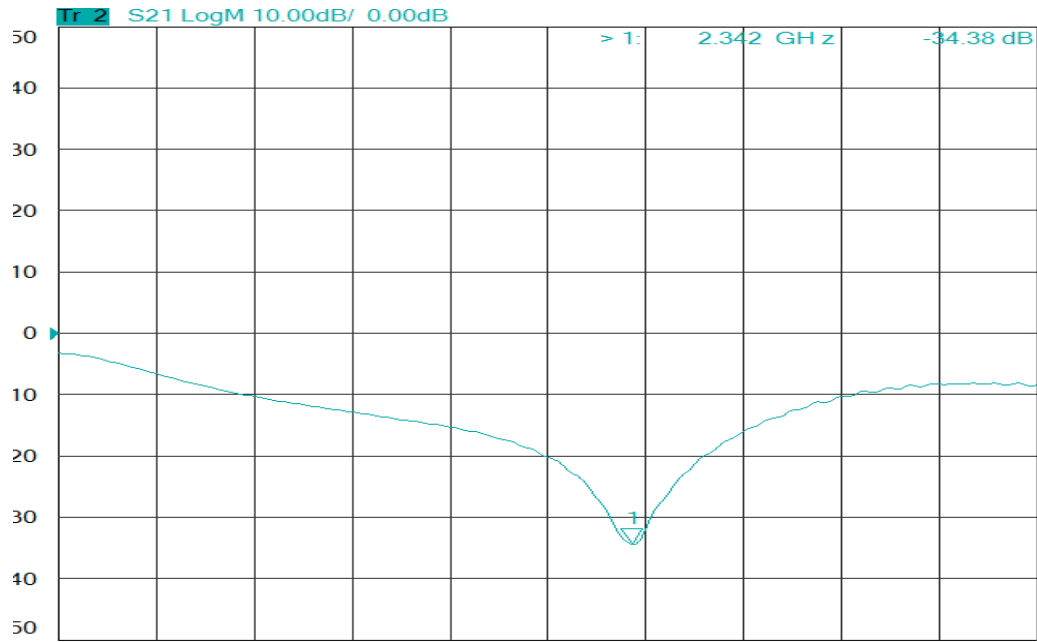


Figure 47a: Isolation (S_{23}) Between the Output Ports 2 and 3 (in dB) vs F (GHz) of Design 1.

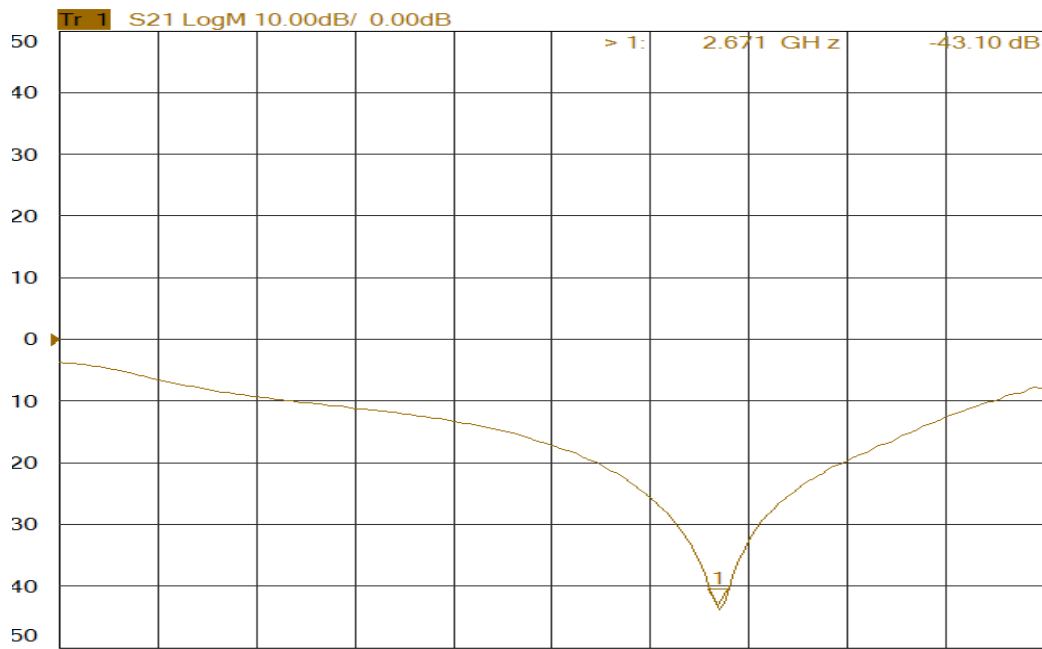


Figure 47b: Isolation (S_{23}) Between the Output Ports 2 and 3 (in dB) vs F (GHz) of Design 2.

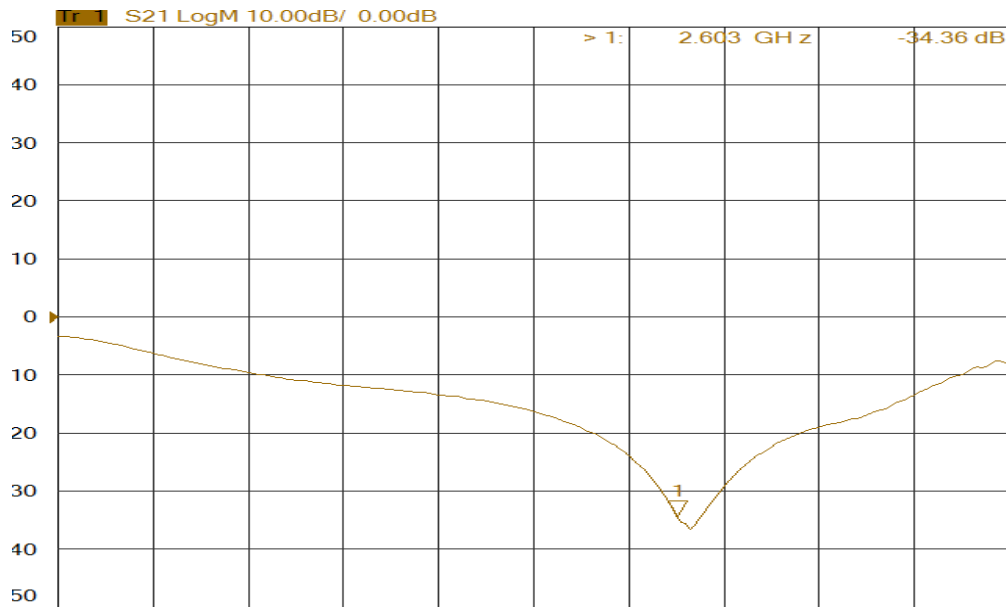


Figure 47c: Isolation (S_{23}) Between the Output Ports 2 and 3 (in dB) vs F (GHz) of Design 3.

The isolation (S_{23}) measured was greater than 30 dB indicating that no power is transferred across the output ports. Although the maximum isolation was observed at different frequencies, the frequency shift might occur due to the fringing field effects, fabrication errors and SMA connector losses at the end of the fabricated boards which might vary the S parameters of the fabricated boards. The measured and simulated results of input return loss, output return loss, insertion loss, isolation versus frequency were approximately similar and all the designs had almost the same performance from the above data. The comparison between the simulated and measured input and output return losses from all divider circuits are shown in Table 13, while the insertion losses are in Table 14 and isolation Table 15.

Table 13: Comparison of Measured and Simulated Return Losses at 2.4 GHz.

S parameters	Power Divider Design	Center Frequency (GHz)		Maximum value (dB)		Frequency Band (>15 dB) (MHz)
		Measured	Simulated	Measured	Simulated	
S ₁₁	Step	2.4	2.347	-24.37	-47.606	1652-3231
S ₁₁	Taper	2.598	2.385	-29.48	-45.560	1585-3251
S ₁₁	Straight	2.500	2.4	-21.67	-40.652	1641-3231
S ₂₂	step	2.40	2.10	-12.88	-67.483	766 -4000
S ₂₂	Taper	2.40	2.166	-18.99	-35.274	735-4000
S ₂₂	Straight	2.125	2.080	-24.12	-29.260	755-4000
S ₃₃	Step	2.316	2.4	-24.49	-41.509	721-4000
S ₃₃	Taper	2.688	2.414	-23.58	-40.100	752-4000
S ₃₃	Straight	2.00	2.4	-20.39	-37.215	683-4000

Table 13 showed that the input return losses of step junction power divider were greater than 15 dB between 1.65 GHz to 3.23 GHz and were maximum at 2.4 GHz and the output return losses had a band of 0.76 GHz to 4 GHz where the power transfer was maximum, and the values were maximum at 2.4 GHz. The tapered junction power divider exhibited better power transfer performance between the frequencies of 1.5 GHz to 3.25 GHz for input return losses and the output return losses were greater than 15 dB within 0.735 GHz to 4 GHz with maximum power transfer at 2.598 GHz and 2.4 GHz respectively. This shows that the step junction also gives better performance like tapered junction and can be used in designing Wilkinson's power dividers.

Table 14: Insertion Losses of Measured and Simulated Power Dividers at 2.4 GHz.

S parameters	Power Divider Design	Maximum value (dB)		S parameters	Maximum value (dB)	
		Measured	Simulated		Measured	Simulated
S_{21}	Step	-3.67	-3.368	S_{31}	-3.74	-3.368
S_{21}	Taper	-3.44	-3.369	S_{31}	-3.51	-3.369
S_{21}	Straight	-3.83	-3.353	S_{31}	-3.77	-3.353

The insertion losses of all the dividers were in the range of 3.3 dB to 3.8 dB and the amplitude balance of these dividers, which is the difference in insertion losses or power divided between port 2 and port 3 were also in the desired range. Also, the power delivered by each power divider was approximately equal to 50% (between 47-49%) indicating almost half of the power was delivered to each output ports from the input port between the frequencies of 0.2 GHz to 4.0 GHz. Since the divider is symmetrical, the values of S_{31} are same as the values of S_{21} . Although the values of straight power divider were fluctuating between 3.3 dB to 3.8 dB, the values of step and tapered power dividers were approximately same.

Table 15: Comparison Between the Measured and Simulated Isolation of Power Dividers

S parameters	Power Divider Design	Center Frequency (GHz)		Maximum value (dB)		Frequency Band (>15 dB) (MHz)
		Measured	Simulated	Measured	Simulated	
S ₃₂	Step	2.342	2.419	-34.38	-45.279	1620-3190
S ₃₂	Taper	2.671	2.465	-43.10	-46.202	1650-3250
S ₃₂	Straight	2.603	2.496	-34.36	-51.235	1690-3301

It was observed from the table that the isolation was greater than 30 dB for all power dividers and the step divider achieved an isolation of 34.38 dB, which is similar to the straight divider. Also, it was observed from the table that the step and straight dividers had good isolation results implying the coupling effects were negligible. Although tapered divider had better isolation among the designs, the difference is minimum. Hence, it can be seen that the measured results were meeting the desired performance of Wilkinson power divider with approximately similar results.

CHAPTER 5

CONCLUSION AND FUTURE SCOPE

This thesis was focused on two principal topics: The use of power combiners to extend the range of Wi-Fi systems and to characterize RF power amplifiers (PAs) on break-out boards without using solder to attach the PA thus allowing for rapid, high-volume characterization of commercial PAs. For the main topic the focus was to simulate, design and test fabricated power dividers while, for the PA testing topic, the goal was to deliver test data to Global ETS, Trinity FL, so that the company could compare measured versus spec data to ensure that non-counterfeit devices were delivered to one of their customers. In this chapter we will first summarize the results from the thesis and then offer some suggestions for possible future work.

5.1 Conclusions

The results presented in Chapter Four indicated that different Wilkinson power divider designs displayed similar performances at the same operating frequency when implemented using microstrip technology. It was also noticed that the step divider had similar results as the straight divider. Since the design and construction of the step divider was simpler, this design can be easily fabricated in microwave industry. The design was robust and easy to use. All the fabricated power dividers exhibited desired return losses greater than 15 dB, insertion losses of approximately 3.3 dB and isolation greater than 20 dB.

The coupling between the transmission lines also influences the odd and even mode impedances of the transmission lines. This depends on the spacing between the transmission lines. As the gap between these lines increases, the impedance varies due to the decrease in capacitance

between the transmission lines and ground, which specifically affects the odd mode impedance. This odd mode impedance decreases depending upon the distance between the lines, also impacting the characteristic impedance of the lines. The formula for the characteristic impedance is given by the formula (5.1).

$$Z_0 = \sqrt{Z_{0e} * Z_{0o}} \quad (5.2)$$

where Z_0 is the characteristic impedance, Z_{0e} is the even mode impedance and Z_{0o} is the odd mode impedance of the device. Depending upon the even and odd mode impedances, the coupling coefficient varies and is given by (5.3)

$$C = \frac{Z_{0e} - Z_{0o}}{Z_{0e} + Z_{0o}} \quad (5.3)$$

The gap between the transmission lines influences the coupling between them. When the gap between the transmission lines decreases, the difference between the even and odd mode impedances increases thereby increasing the coupling between the transmission lines [13]. Since Wilkinson's power divider can also be used as a power combiner due to reciprocity, the coupling between the transmission lines is negligible since the gap between the transmission lines is not an important factor. This indicated that the divider is acting in even mode and transferred signals have the same amplitude and are in phase

It was also observed that since tapered quarter wavelength dividers were mostly used, step junction power dividers can also be used in designing a Wilkinson power divider. Thus, the performance of the step junction divider was comparable and approximately equal to the tapered divider and had better return losses. Although the tapered power divider had greater isolation, the isolation of the step and straight power dividers were greater than 30 dB, resulting in the same performance as the tapered divider. The variation of dielectric constant of these dividers could be due to fabrication errors since the milling depth of the Cu board was adjusted manually on the

milling machine. However, the dividers had similar performance indicating that the variation in the dielectric constant does not impact the performance of the power dividers.

The measured results of the power dividers were satisfactory and approximately the same, with some properties better for one design than the other. The fabricated tapered power divider had better input and output return losses of 30 dB and 19 dB, respectively, but with lower isolation between the output ports when compared to the straight power divider. The bandwidth was also better for the tapered divider when compared to the step and straight power dividers. However, the step power divider provided better input and output return losses at a center frequency of 2.4 GHz and was easier to construct.

A scattering matrix can be derived for each of the power divider types. Here only the magnitude of the S parameters was considered as this best illustrates differences in the anticipated performance of each power divider derived from the S matrix elements in Tables 13, 14 and 15.

$$\text{Step Divider} = [S] = \frac{1}{\sqrt{2}} \begin{bmatrix} 0.003 & 0.89 & 0.93 \\ 0.89 & 0.09 & 0.10 \\ 0.91 & 0.10 & 0.11 \end{bmatrix} \quad (5.4)$$

$$\text{Tapered Divider} = [S] = \frac{1}{\sqrt{2}} \begin{bmatrix} 0.008 & 0.972 & 0.97 \\ 0.973 & 0.19 & 0.24 \\ 0.97 & 0.009 & 0.21 \end{bmatrix} \quad (5.5)$$

$$\text{Straight Divider} = [S] = \frac{1}{\sqrt{2}} \begin{bmatrix} 0.008 & 0.871 & 0.962 \\ 0.94 & 0.009 & 0.18 \\ 0.963 & 0.18 & 0.06 \end{bmatrix} \quad (5.6)$$

The matrices show that the dividers have similar performance at the operating frequency of 2.4 GHz. Since the performance of each power divider was similar, any topology could be used to design a Wilkinson's power divider.

A conclusion can be drawn that the tapered divider also had better input and output return losses, good isolation between the output ports and better power division between the input and output ports. But, this design is complicated when compared to the step divider and there were

non-negligible variations between the simulated and experimental values when compared to the step divider.

The designs were all compared, and it was deduced that any design can be implemented to design a power divider with microstrip technology for a reasonable frequency under 10 GHz and same performance can be expected from these dividers. Parallel dividers are equally efficient as curved dividers and the parameters of the step junction power divider, tapered power divider and straight power divider were similar. But step junction power divider was easy to manufacture and could be understood easily.

5.2 Future Work

This section is divided into two parts: First a discussion of how power dividers can be used to boost Wi-Fi signals without the use of RF repeaters, and second how the designs presented here might be improved to achieve higher-performance Wilkinson power dividers.

5.2.1 Applications of Power Dividers in the RF and Microwave Industry

We know that power dividers are being used in the Wireless Industry for transmission and receiving purposes in transceiver circuits, to boost the Wi-Fi signals, and to increase mobile signal coverage in cellular repeater circuits. They can also be used for dual-band applications with broad bandwidth and are also used in high power amplifier circuits. A power divider is also used in WLAN applications to divide the input signals to feed an array of antennas. We can design 1:2N power dividers, where N stands for the number of ports, which is used as a feed network for devices like phase array antennas, RF communications, etc. Although we know that as the number of output ports increases, isolation between them decreases so it is important that the desired isolation of more than 15 dB criteria be maintained. A block diagram of N-way power dividers is shown in the Figure 48, which can be used as a feeding circuit for many applications.

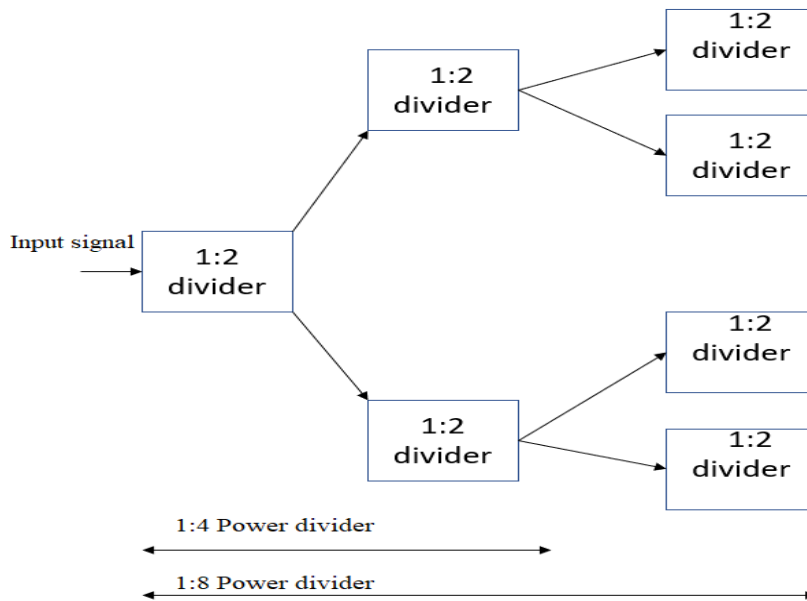


Figure 48: Block Diagram of N-way Power Divider used as a Feed Network.

Each basic block is a standard Wilkinson power divider and the blocks are cascaded to achieve a high N. Power combiners are employed to boost the power of the signal sent by a wireless modem (or Wi-Fi modem) to a Wi-Fi connected device, thus forming a two node Wi-Fi network. When the two nodes are not in proximity to each other, or more commonly have a variable range between them, the Wi-Fi link may be maintained by ensuring that adequate transmit/receive power is used. The combiner does this by boosting the output power of both nodes. In fixed node applications this is best done using repeaters, which can be configured easily. However, for simple networks where fixed repeaters are not practical, another Wi-Fi network solution is needed. Note that the power level of the wireless signals must be in the range of -30 to -70 dBm to have adequate signal strength, thus allowing users to access the network. Any drop in the power level weakens the signal connection and thus degrades link bandwidth. Using devices such as power combiners and RF switches to adjust the transmit power of each node can ensure adequate transmit power thus maintaining link fidelity. Also, due to reciprocity, the power divider can be used as a power

combiner. In this case the combiner has less losses when both output ports are driven with an equal amplitude and at the same phase as shown in Figure 49.

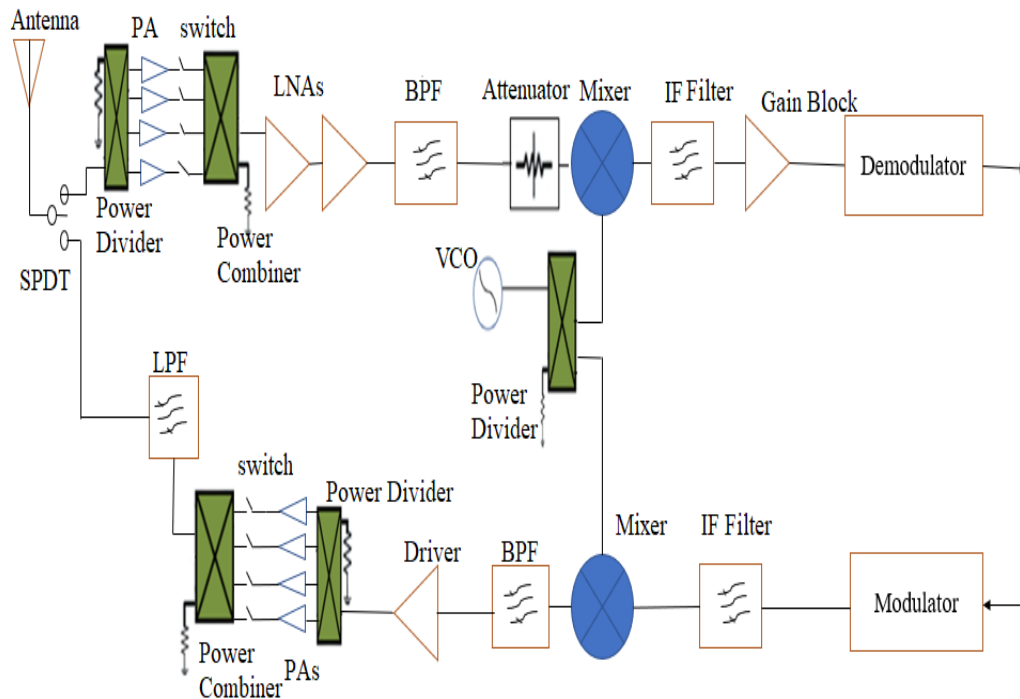


Figure 49: Power Combiner/Divider in a Wi-Fi Transceiver Circuit to Boost the Wi-Fi Signals and to Establish the Wi-Fi Link when the Transmitter/Receiver are Mobile.

5.2.2 Possible Power Divider Improvements

Although the dimensions of all the fabricated power divider boards were 49×23 mm, more compact divider boards are needed, and active research is going on to provide the desired performance on compact fabricated boards [23]. Some of the new technologies for designing Wilkinson's power divider includes miniaturizing the size while functioning in dual bands and using stepped impedance lines and open stubs [24]. Also, other power combiners such as rat race couplers can also be used to provide better power division with three (3) quarter wavelength transmission lines ($\lambda/4$) and one (1) three quarter wavelength transmission line ($3\lambda/4$) with four ports. Since the input ports do not have any lumped elements, the parasitic effects are less when compared to the Wilkinson's power divider [25]. The rat race couplers are used to combine two

in-phase signals with approximately no losses and to split the input signal without any phase difference between the output ports. A typical rat race coupler is shown in Figure 50.

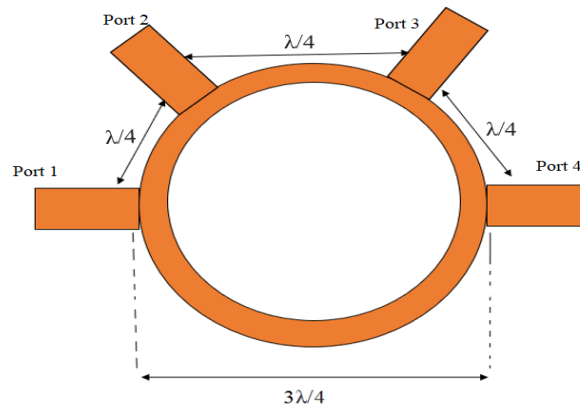


Figure 50: The Layout of a Typical Rat Race Coupler.

The input signal at Port 4 is divided into Ports 1 and 3 while Port 2 is isolated. Hence, Port 4 is referred as sum port while Port 1 is the delta port. For an ideal rat race couplers, equal power split of 3 dB is observed only at the operating frequency. Ports 2 and 4 has an 180° phase difference

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